



Electronic structure theory of the hidden-order material URu₂Si₂

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We report a comprehensive electronic structure investigation of the paramagnetic (PM), the large moment antiferromagnetic (LMAF), and the hidden order (HO) phases of URu₂Si₂. We have performed relativistic full-potential calculations on the basis of the density-functional theory, employing different exchange-correlation functionals to treat electron correlations within the open 5*f* shell of uranium. Specifically, we investigate—through a comparison between calculated and low-temperature experimental properties—whether the 5*f* electrons are localized or delocalized in URu₂Si₂. The local spin-density approximation (LSDA) and generalized gradient approximation (GGA) are adopted to explore itinerant 5*f* behavior, the GGA plus additional strong Coulomb interaction (GGA+*U* approach) is used to approximate moderately localized 5*f* states, and the 5*f*-core approximation is applied to probe potential properties of completely localized uranium 5*f* states. We also performed local-density approximation plus dynamical mean-field theory calculations (DMFT) to investigate the temperature evolution of the quasiparticle states at 100 K and above, unveiling a progressive opening of a quasiparticle gap at the chemical potential when temperature is reduced. A detailed comparison of calculated properties with known experimental data demonstrates that the LSDA and GGA approaches, in which the uranium 5*f* electrons are treated as itinerant, provide an excellent explanation of the available low-temperature experimental data of the PM and LMAF phases. We show furthermore that due to a material-specific Fermi-surface instability a large, but partial, Fermi-surface gapping of up to 750 K occurs upon antiferromagnetic symmetry breaking. The occurrence of the HO phase is explained through dynamical symmetry breaking induced by a mode of long-lived antiferromagnetic spin fluctuations. This dynamical symmetry breaking model explains why the Fermi-surface gapping in the HO phase is similar but smaller than that in the LMAF phase and it also explains why the HO and LMAF phases have the same Fermi surfaces yet different order parameters. A suitable order parameter for the HO is proposed to be the Fermi-surface gap, and the dynamic spin-spin correlation function is further suggested as a secondary order parameter.

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I. INTRODUCTION

Over the past 15 years the concept of “hidden order” (HO) has evolved to describe the emergent behavior of various quantum or strongly correlated materials where the order parameter (OP) of a clear phase transition along with its elementary excitations remain unknown. Often modern microscopic measurement techniques of diffraction (neutrons or photons), nuclear magnetic resonance (NMR), or muon spin rotation (μ SR), etc., are unable to detect and characterize the new ordered phase. Yet the thermodynamic and transport properties unambiguously discern a novel state of matter appearing at a sharp transition temperature. Within this state additional unconventional phases may form depending on varying parameters such as pressure, magnetic (electric) fields, and doping. Although there is at present no comprehensive review of the generic HO problem and its relation to quantum criticality, the HO concept is beginning to make headway into the recent literature.^{1–6}

A prototype system for this behavior is the intermetallic compound URu₂Si₂, discovered 25 years ago.^{7–9} This material displays strong electron correlations such that the U 5*f* magnetic moments are dissolved into hybridized bands near the Fermi surface (FS) and a moderately heavy Fermi liquid forms at temperatures below approximately 70 K.^{10,11} Then at 17.5 K the HO state appears via a dramatic (second-order)

phase transition.^{7–9} The above-mentioned techniques fail to discern the order parameter and cannot characterize its elementary excitations. Great attention has been devoted to studying this system with the aim of uncovering its hidden nature. A vast collection of experimental data has been gained and excellent single crystals are now available for definitive investigations thereby eliminating extrinsic effects of impurities and stress (see, e.g., Ref. 12). In addition there are numerous theoretical proposals and exotic models spanning many years^{13–28} that have, however, not come to full grips with many aspects of the experimental behavior.

Recent investigations^{12,29–33} on good single crystals have mapped out the phase diagram of URu₂Si₂. Apart from the paramagnetic (PM) phase and the HO phase below 17.5 K at ambient pressure, there is also the large moment antiferromagnetic (LMAF) phase, which appears with modest pressure of about 0.5 GPa and is characterized by uranium moments of 0.4 μ_B in a type-I AF arrangement. Surprisingly, the bulk properties of the HO and LMAF phases are very much alike. Very similar, continuous changes in the thermodynamic and transport quantities have been reported for both phases.^{12,30,31,34,35} A comparable Fermi-surface gapping occurs for the transitions from the PM phase to the HO and LMAF phases, respectively. This similarity—which has been called adiabatic continuity³⁶—extends to the Fermi surfaces of the HO and LMAF phases. De Haas–van Alphen (dHvA)

experiments detect no significant differences between the Fermi surfaces of the HO and LMAF phases³⁷ and, consistently, neutron-scattering experiments find the same nesting vectors.³⁸ Nonetheless, the HO and LMAF unmistakably have different order parameters; simple magnetic order in the LMAF phase but an unknown order parameter in the HO phase. Neutron and x-ray scattering experiments^{39–43} detected a small magnetic moment $\sim 0.03 \mu_B$ in the HO phase but this small moment is currently considered as a parasitic moment that is not intrinsic to the HO phase.^{12,33,44} Other differences between the HO and LMAF phases is that below 1.2 K and only out of the HO an unconventional⁴⁵ superconducting (SC) state appears, which is the subject of recent interest.^{46–48} A further salient difference between the HO and LMAF phases is that inelastic neutron experiments detected a mode of AF spin fluctuations in the HO phase which freezes to the static antiferromagnetic Bragg peak in the LMAF phase.^{35,38,42}

As a starting point toward a full theoretical understanding of the intriguing electronic structure of URu_2Si_2 state-of-the-art band-structure calculations are required. We present here detailed investigations of the electronic structures of the PM and LMAF phases, using various computational methods. On the basis of the obtained electronic structures, we analyze in how far the known physical properties of URu_2Si_2 can be explained from these underlying electronic structures, and draw conclusions on what the valid electronic structure of URu_2Si_2 is, emerging from the electronic structure calculations. Subsequently, we focus on the implications for a prospective explanation of the HO. Also, we expand on the “dynamical symmetry-breaking” model for the HO, which we have recently proposed.²⁴ Details of this model are given and we relate the model to a larger collection of experimental properties. We also compare the derived electronic structure and the HO model to other recent proposals. In the following we first consider an issue that is central to the current discussion of model explanations of the HO phase.

II. ITINERANT OR LOCALIZED $5f$ BEHAVIOR?

One of the most intriguing questions regarding the electronic structure of URu_2Si_2 , and consequently the explanation of the HO, is whether the uranium $5f$'s are localized or delocalized. Single-ion theories of the HO, such as, e.g., quadrupolar or octupolar ordering, are based on the assumption of localized $5f$'s.^{14,16,19,21,23,26,28,49–52} This important issue of the degree of $5f$ localization has been controversially discussed recently. Several theories adopt the picture of localized $5f$ states from the outset, however, an examination of the grounds for this is needed. A thorough examination seems to unveil that there is little compelling experimental evidence for localized $5f$'s. Smoking-gun evidence for localized f states would be the classical observation of crystal electrical field (CEF) f excitations in neutron experiments but only itinerant spin excitations have been detected and CEF excitations have never been observed for URu_2Si_2 (see, e.g., Ref. 53). Another indication of a CEF excitation could, e.g., come from measured specific-heat curves in which humps or peaks could signal the occurrence of CEF excita-

tions. The measured C/T curve of URu_2Si_2 shows a maximum at 70 K,⁸ which has sometimes been interpreted as evidence for a CEF transition. However, later measurements⁵⁴ of the C/T of ThRu_2Si_2 , which has no occupied $5f$'s and hence no CEFs, revealed a very similar maximum at the very same temperature. This suggests that the peak at 70 K is more likely related to the same underlying lattice structure and not to a CEF transition of $5f$ states. The shape of the measured magnetic entropy $S_m(T)$ in the PM state does not correspond to Schottky-type anomaly expected for CEF levels.^{54,55} Also, very recent scanning tunneling spectroscopy (STS) measurements could not detect any CEF splitting of the $5f$'s.⁵⁶ Consistently, the susceptibility of URu_2Si_2 does not show Curie-Weiss behavior near the HO temperature that might indicate localized f states, rather Curie-Weiss behavior commences only above 150 K.^{7,57}

One particular piece of experimental evidence in favor of localized $5f$'s has come from inelastic neutron-scattering experiments⁵⁸ in which a small inelastic peak was observed at 363 meV. This peak has been interpreted as a signature of an intermultiplet transition.⁵⁸ A similar peak has been observed for UO_2 , which is indeed known to have a localized $5f^2$ configuration. However, for UO_2 CEF excitations, too, were definitely observed with inelastic neutron scattering (see, e.g., Ref. 59). The inelastic neutron experiments⁵⁸ also detected a small peak at 363 meV for ThRu_2Si_2 , which indicates that the peak might in fact not be due to an intermultiplet excitation. In addition, a similar peak has been observed⁶⁰ for URhAl , which is however known to be an itinerant $5f$ material.⁶¹ The origin of the neutron peak at 380 meV in URhAl has consequently been debated,⁶² the issue is not completely solved but it could be an artifact related to the measurement apparatus.

Several other experimental data rather advocate the existence of delocalized $5f$ electrons in URu_2Si_2 . High-resolution photoemission spectroscopy (PES) using He I and He II radiation gave evidence for a typical delocalized $5f$ response in the He II-He I difference spectrum.⁶³ A similar difference spectrum has been observed for itinerant U metal and UGa_3 .⁶⁴ In addition, angular-resolved PES (ARPES) revealed dispersive bands in URu_2Si_2 ,^{65,66} yet it still needs to be clarified what the dominant character of the observed bands is (f related or not). On the other hand, very recent He I ARPES measurements provided a picture of an almost flat band which sinks through E_F at the HO transition.⁶⁷ The picture of a narrow band very close to E_F may however arise from the special data treatment, i.e., division by the Fermi function and double-differentiation technique, which always tends to give an impression of a flat state near E_F .

A recent electron energy-loss spectroscopy (EELS) study⁶⁸ deduces for the $5f$ states in URu_2Si_2 the intermediate coupling mechanism to be valid, which might imply a tendency to f localization, or perhaps a dual, i.e., both itinerant and localized (see, e.g., Ref. 69), nature of the f electrons. However, an unambiguous connection between the atomic coupling scheme and degree of f localization has not yet been established.

The AF phase of URu_2Si_2 is commonly referred to as the large moment antiferromagnetic phase. This name suggests that the $5f$'s in the LMAF phase might be partially localized.

However, in spite of its name, the uranium moment in the LMAF phase is actually relatively small and not the typical moment of a localized $5f$ material. For example, the $5f$ states of the cubic uranium salt USe are known to be closer to $5f$ localization, but still exhibit some f - d hybridization, which leads typically to spin, orbital, and total moments of $-1.1 \mu_B$, $3.1 \mu_B$, and $2.0 \mu_B$, respectively, for USe.⁷⁰ The total moment on U in AF URu₂Si₂ is with $0.4 \mu_B$ quite far from such value. Instead, the U moment is much closer to values of $0.6 \mu_B$ measured for an itinerant $5f$ material such as UGa₃.⁷¹

It also deserves to be mentioned that the results of recent positron annihilation experiments on URu₂Si₂ proved to be incompatible with localized f 's but are on the contrary in good agreement with delocalized f 's.⁷² Also, recent neutron-scattering experiments detected itinerant $5f$ spin excitations.⁵³

Altogether, there does not appear to be clear, compelling evidence for localization of $5f$ electrons in URu₂Si₂. On the other hand, there exists a body of evidence in favor of delocalized $5f$'s. Nonetheless, the decision on localized-itinerant behavior should be concluded from an extensive comparison of calculated and experimental properties, which will be presented below.

In the following section we first outline the here-to-be applied first-principles based techniques to study the electronic structure of URu₂Si₂. With these different approaches we can treat the full range of $5f$ behavior, from delocalized to localized. In view of the above considerations regarding the itinerant or localized $5f$ behavior, our main focus will be on the $5f$ band description. The applied density-functional theory (DFT)-local spin-density approximation (LSDA) and LSDA+ U approaches can provide only ground-state $T=0$ K properties. The temperature dependence of quasiparticle spectra will be treated through dynamical mean-field theory (DMFT) calculations.

III. COMPUTATIONAL METHODOLOGY

Our calculations are based on the DFT as well as on the DMFT. Specifically, for the treatment of the DFT static exchange-correlation potential we have employed the LSDA,⁷³ the generalized gradient approximation (GGA),⁷⁴ and also orbital-dependent extensions (LSDA+ U and GGA+ U) to include the influence of strong on-site Coulomb correlations.

In our calculations we have used three accurate full-potential, relativistic electronic structure codes. These are the full-potential local orbitals (FPLO) method^{75,76} and the full-potential linearized augmented plane-wave (FLAPW) method; the latter we employed both in the WIEN2K (Ref. 77) and KANSAI implementations. We have verified that the three codes give, on the self-consistent local-density approximation (LDA) level, *identical* results for the electronic structure of nonmagnetic URu₂Si₂. WIEN2K and FPLO have been verified to provide identical results for the LMAF phase.

In the FLAPW calculations the relativistic valence states are computed within the full, nonspherical potential. The relativistic spin-orbit interaction was included

self-consistently,⁶² and, in the WIEN2K calculations, we used the relativistic local orbitals extension of the scalar-relativistic FLAPW basis to treat accurately the $2p_{1/2}$ semicore states.⁷⁸ The product of R_{mt} and maximum reciprocal space vector (K_{\max}), i.e., the basis size determining parameter (RK_{\max}) was set to 7.5 and the largest reciprocal vector G in the charge Fourier expansion, G_{\max} , was equal to 12. We used about 5000 k points for self-consistent convergence. With the WIEN2K calculations we have employed the orbital-dependent GGA+ U method with around mean-field double-counting correction,⁷⁹ in which an additional on-site Coulomb interaction, expressed by the Hubbard U and exchange J parameters, is introduced for the $5f$ states manifold.

In the relativistic full-potential FPLO calculations⁷⁶ the four-component Kohn-Sham-Dirac equation, which implicitly contains spin-orbit coupling up to all orders, is solved self-consistently. We note that the relativistic Kohn-Sham-Dirac approach does not assume any atomic type of angular momentum coupling mechanism, rather the coupling follows from the self-consistent calculation. With the relativistic FPLO and FPLAPW implementations we are normally in the intermediate coupling regime for uranium intermetallics. In the FPLO calculations we used the following sets of basis orbitals: $5f$; $6s6p6d$; $7s7p$ for U, $4s4p4d$; $5s5p$, and $3s3p3d$, for Ru and Si, respectively. The high-lying $6s$ and $6p$ U semicore states, which might hybridize with other valence states are thus included in the basis. The site-centered potentials and densities were expanded in spherical harmonic contributions up to $l_{\max}=12$. Brillouin zone (BZ) sampling was performed with maximally $20 \times 20 \times 20$ k points.

For the DMFT calculations we have used a recently developed⁸⁰ full-potential, relativistic LDA+DMFT method. For a detailed review of the DMFT method we refer to Ref. 81. In our DMFT calculations we use the spin-polarized T-matrix fluctuation-exchange (FLEX) impurity solver^{82,83} for generating the self-energy. This impurity solver is expected to be applicable to moderately correlated materials, as, e.g., uranium intermetallic compounds. The local Green's function is computed employing Kohn-Sham states which are obtained from a relativistic LDA calculation. The Coulomb U and exchange J quantities of the DMFT part are connected to the two-electron integrals of the Coulomb interaction of the f electrons through the effective Slater integrals $F_{2\kappa}$ ($0 \leq \kappa \leq 3$), where $F_0=U$, $F_4=\frac{41}{297}F_2$, $F_6=\frac{175}{11583}F_2$, and $J=\frac{286F_2+195F_4+250F_6}{6435}$. In the DMFT calculation we used 8192 Matsubara frequency points to compute the temperature-dependent quasiparticle spectrum, which was obtained using a Padé approximation to the frequency-dependent lattice Green's function $G(k, i\omega)$. Within the present DMFT FLEX implementation temperatures down to about 100 K can only be reached.

In our investigations we employ the ThCr₂Si₂-type body-centered tetragonal (bct) structure with space group No. 139 for paramagnetic URu₂Si₂ and the simple tetragonal (ST) structure with space group No. 123 for AF URu₂Si₂. The ST unit cell volume of AF URu₂Si₂ is twice the bct unit-cell volume of PM URu₂Si₂. The space group of the HO phase has not yet been definitely established because the symmetry breaking in the HO phase is as yet to be unveiled. In Fig. 1

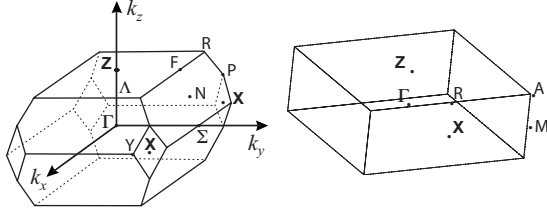


FIG. 1. The Brillouin zones of the body-centered tetragonal phase (space group No. 139, left) and the simple tetragonal phase (space group No. 123, right) with high-symmetry points indicated (Ref. 84).

the Brillouin zones of the bct and ST structures are shown with high-symmetry points indicated. The ST BZ corresponds to a main folding of the bct BZ at $\pm \frac{1}{2}Z$ and smaller folding along the X-X axes. In the bct BZ we have additionally labeled several nonhigh-symmetry points (Σ , Φ , Ψ , and Λ) for later discussion.

IV. RESULTS

A. DFT delocalized 5f electron calculations

1. Structural optimization

To start with, we consider the structural properties of URu_2Si_2 , that is, the equilibrium lattice coordinates, bulk modulus, and equation of state. Several experimental investigations of the structural properties of URu_2Si_2 have been reported.^{7,85–87} For comparison to the available data, we have performed *ab initio* optimizations of the equilibrium volume, the c/a ratio, and the internal Si coordinate, z_{Si} . These optimizations have been performed on the LSDA level, both for the PM and LMAF phases. In Fig. 2 we show the computed total energy versus unit-cell volume. Both PM and LMAF total energies are given for the ST cell, to convene comparing the two phases. The theoretically predicted equilibrium

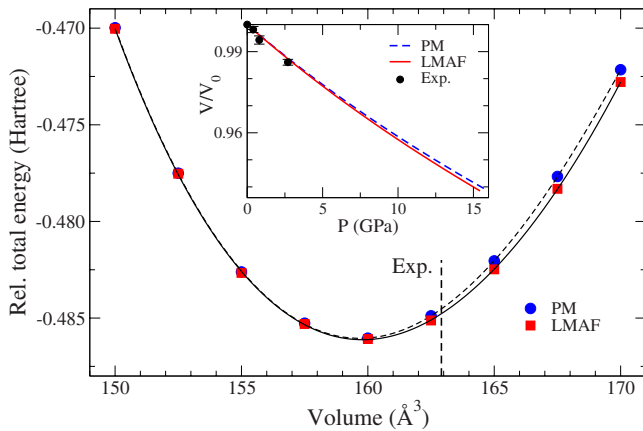


FIG. 2. (Color online) The *ab initio* computed total energy versus volume for the PM and LMAF phases of URu_2Si_2 . The vertical dashed line indicates the experimental equilibrium volume (Ref. 85), the inset shows the *ab initio* computed pressure dependence of the unit-cell volume for the PM and LMAF phases, normalized to the zero-pressure volume V_0 , together with experimental data points of Ref. 87.

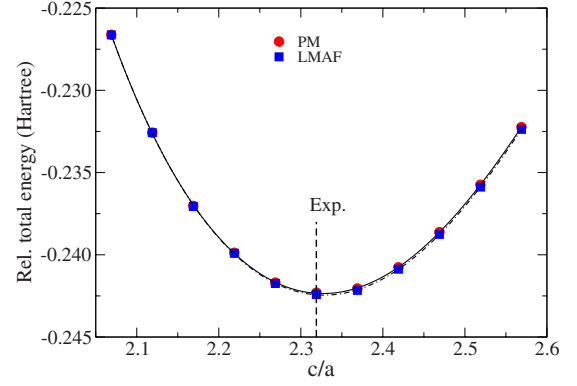


FIG. 3. (Color online) Total-energy optimization of the c/a ratio of URu_2Si_2 for the PM and LMAF phases. The dashed vertical line denotes the experimental value (Refs. 7 and 85).

unit-cell volume is about 1.7% smaller than the experimental volumes, which are 162.9 \AA^3 (Refs. 7 and 85) and 162.6 \AA^3 (Ref. 87), respectively. Hence, the theoretical value is in very good agreement with experiment. As Fig. 2 illustrates the total energies of the PM and LMAF phases are very near one another. The total energy of the LMAF phase is computed to be only 7 K/f.u. deeper than that of the PM phase. This is in itself a remarkable finding, which appears to be a specific feature of URu_2Si_2 . The inset of Fig. 2 presents the computed volume versus pressure dependence of URu_2Si_2 . With pressure the antiferromagnetic state becomes slightly more stable. The inset includes recent experimental data points of Ref. 87. A fit of the computed volume versus pressure curves gives a bulk modulus B_0 of 204 GPa (208 GPa) for the LMAF (PM) phase. The recent pressure experiment⁸⁷ obtained a value of 190 GPa; an older experiment reported a value of 230 GPa.⁸⁸

The optimized theoretical c/a ratio is shown in Fig. 3. The obtained theoretical c/a ratio almost coincides with the experimental value (2.32).^{7,85} The optimized c/a ratio of the LMAF phase is found to be just a small fraction larger than that of the PM phase. We note that x-ray diffraction experiments have been unable to detect any difference in the lattice constants of the PM, LMAF, and HO phases.^{87,89} Only dilatation experiments^{33,86} could so far detect tiny differences in both the a and c lattice constants of the three phases; the c axis lattice constant of the LMAF and HO phases are elongated with a few parts in 10^{-5} , as compared to the PM phase (at higher temperature). The a axis of the HO and LMAF phases is contracted by a few parts in 10^{-5} . As a result, the c/a ratio increases⁸⁶ with about 10^{-4} from the PM above 17.5 K down to the LMAF phase at 10 K. The optimized c/a ratio of the LMAF phase is consistently computed here to be about 10^{-4} larger than that of the PM phase, in agreement with experiment.⁸⁶ We refrain however from a more detailed comparison because we cannot make a meaningful quantitative statement for such tiny numbers.

Using the optimized c axis lattice constant and volume, the theoretical a axis lattice constant is about 0.6% smaller than the experimental value.^{7,85,87} As the LSDA approach is known to produce a small overbinding, the correspondence with the experimental lattice constant can be regarded as very good.

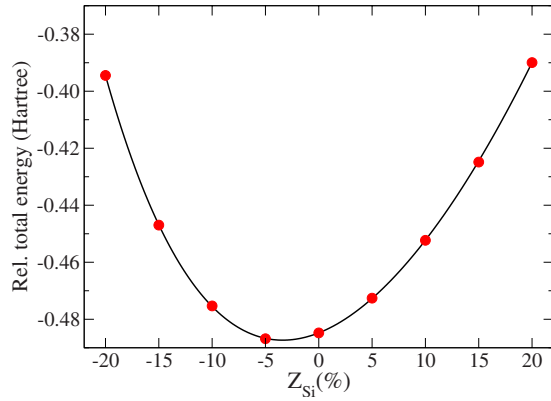


FIG. 4. (Color online) Total-energy optimization of the special Si z position in URu_2Si_2 . The zero position of z_{Si} is taken at 0.371 (Ref. 85).

The bct structure of URu_2Si_2 has one internal coordinate, the Si z position. Results for the total-energy optimization of the z_{Si} coordinate are given in Fig. 4. The theoretical LSDA value is found to be 3% smaller than the experimental value of 0.371 (Ref. 85). A more recent experiment⁸⁷ obtained a somewhat smaller z_{Si} value, 0.3609, which would agree quite well with our theoretical result. As will be shown in more detail below, the essential physical properties of URu_2Si_2 are stable with respect to moderate variations in the unit-cell dimensions and the internal z_{Si} coordinate.

Altogether, the *ab initio* structural optimization shows that the crystallographic properties of URu_2Si_2 are well described by the LSDA approach, which intrinsically is based on the assumption of itinerant $5f$ electrons. It is known from computational investigations for other actinide materials that, when these have $5f$ states that are localized, the LSDA approach usually does not provide a good description of the lattice properties (see, e.g., Ref. 90). Such deviant behavior is not found here for URu_2Si_2 .

2. Energy band dispersions

We first consider the outcome of LSDA $5f$ -itinerant calculations for the electronic structure of URu_2Si_2 . In Fig. 5 we show the computed LSDA energy dispersions in the PM and LMAF phases for the experimental lattice parameters.⁸⁵ To draw a comparison, both sets of dispersions are given for the double unit cell (space group No. 123). As has been noted recently by us, the energy dispersions of these two phases are very similar.²⁴ The dispersions of the AF phase are almost on top of those of the PM phase, except for some influence of the exchange splitting of $5f$ -related bands. This finding corroborates fully with the compute tiny total-energy difference between these two phases. A degeneracy of crossing bands occurs near the Fermi level, as can be recognized along the Γ -M and X- Γ symmetry directions. The degenerate band crossing, existing in the PM phase along the Γ -M direction just below E_F , is lifted in the LMAF phase, due to a rehybridization, and thereby a small gap opens. A similar degenerate crossing point along the X- Γ direction is however not removed in the LMAF phase. Through a larger part of the BZ degenerate crossings of the two bands exist, yet the open-

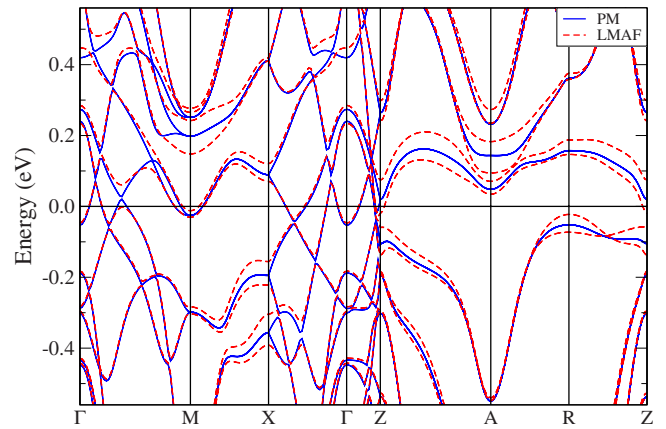


FIG. 5. (Color online) Computed LSDA energy dispersions of URu_2Si_2 in the PM and LMAF phases, both are shown, for sake of comparison, in the simple tetragonal BZ.

ing of a gap in the AF phase does not happen uniformly over the FS.²⁴ This gapping is related to a FS instability of URu_2Si_2 in the PM phase, where degenerate band crossing (Dirac points) occur off the high-symmetry directions, between the Γ -M and Γ -X directions. These degenerate points, which are closely related to the Fermi-surface hot spots discussed below, are removed in a transition to the LMAF phase, leading to a k -dependent FS gapping that is largest in the $z=0$ plane.²⁴

An enlarged view of the PM and LMAF energy bands along the Γ -M direction is shown in Fig. 6. In addition we have highlighted the orbital character of the bands through the colors and the amount of orbital character through the thickness of the bands. Ru $4d$ character is shown by the light grey shading (green color in online version); the bands that consist primarily of Ru $4d$ character appear about 0.20 eV below E_F . The bands closer to the Fermi energy contain dominantly U $5f$ character, as is shown by the medium grey shading (online: blue color) in the PM phase and the dark

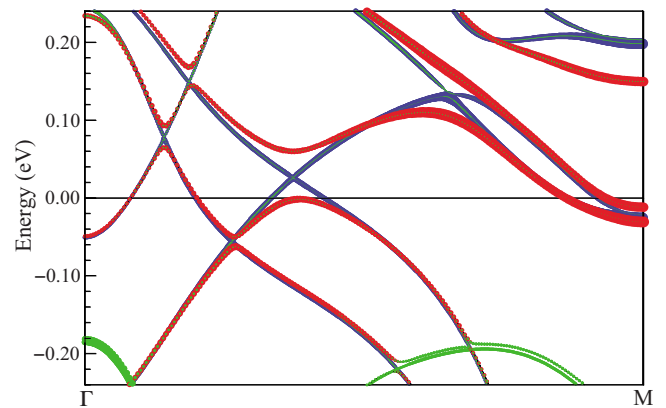


FIG. 6. (Color online) Enlarged view of the PM and the LMAF bands along the Γ -M (Σ) high-symmetry direction in the simple tetragonal BZ. The character of the LSDA bands is given through the color of the bands [light grey (green): Ru $4d$, dark grey (red): U $5f$ in LMAF phase, and medium grey (blue): U $5f$ in PM phase]. The amount of Ru $4d$ or U $5f$ character in the respective bands is given by the thickness of the bands.

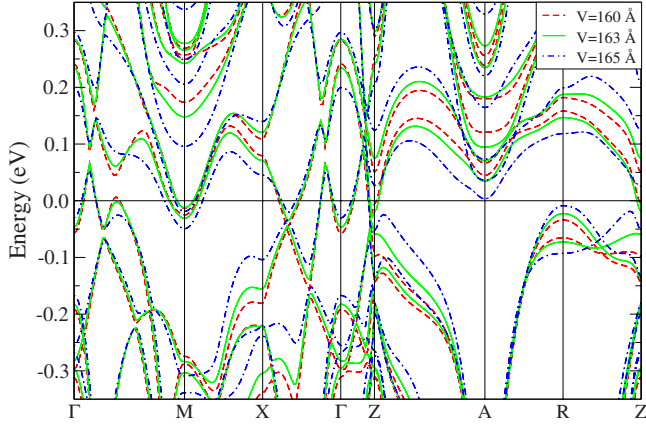


FIG. 7. (Color online) Computed LSDA energy dispersions of antiferromagnetic URu_2Si_2 for several unit-cell volumes around the experimental volume (162.9 \AA^3).

grey shading (online: red color) in the LMAF phase. A small admixture of Ru d character is nevertheless present. The lifting of the degenerate band crossing is clearly borne out uranium $5f$ dominated states. The bands with mainly Ru $4d$ character are unaffected. The gap opening due to the rehybridization of states in the LMAF phase is about 60 meV wide and located in a narrow reciprocal space region at a distance of about $0.25a^* - 0.3a^*$ from the Γ point. These values agree well with those observed in recent STS measurements.⁹¹

URu_2Si_2 is known to be a compensated metal (see, e.g., Refs. 46 and 92). The LSDA-computed energy bands of URu_2Si_2 (Fig. 5) are fully consistent with the property, as has been pointed out recently.^{24,72} Both the opening of the gap in the symmetry-broken phase and the compensated metal character are closely connected to the uranium $5f$ occupancy. Our LSDA calculations predict a $5f$ occupancy of 2.7,⁹³ a value which is consistent with recent EELS measurements.⁶⁸

The lifting of a FS instability in the LMAF phase is a significant feature of URu_2Si_2 obtained from *ab initio* calculations. The gap appearing around the Fermi level is narrow and might therefore sensitively depend on the lattice constants. In Fig. 7 we show the influence of the volume on this feature. For a range of volumes about the experimental volume the gapping property is found to be stable. We have similarly investigated the influence of the z_{Si} coordinate on the FS gapping (not shown). Also for the z_{Si} coordinate we find that the gapping property is stable for a range of values around the experimental one.

To end this LSDA/GGA band-structure section we briefly mention that several LSDA electronic structure calculations have been reported for URu_2Si_2 .^{92,94–96} Rozing *et al.*⁹⁵ and Ohkuni *et al.*⁹² reported LDA calculations for PM URu_2Si_2 , Yamagami and Hamada⁹⁶ reported LSDA calculations of antiferromagnetic URu_2Si_2 . The nonfull-potential calculations^{92,95} for the PM phase are in reasonable agreement with our full-potential results. Our energy bands and FS of AF URu_2Si_2 are however distinctly different from earlier published results.⁹⁶ A reason for this difference is not known. As mentioned before, we have verified that independent state-of-the-art electronic structure codes give nearly identi-

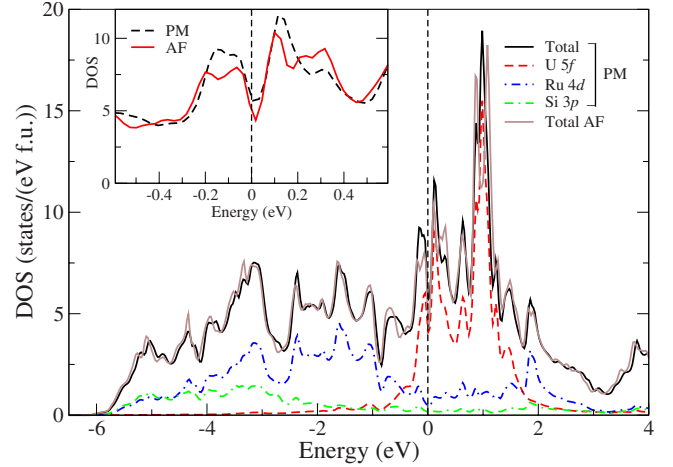


FIG. 8. (Color online) Partial DOS of URu_2Si_2 in the paramagnetic and large moment antiferromagnetic phases. The inset shows an enlargement of the PM and AF DOS around the Fermi energy (at 0 eV), illustrating the partial gapping occurring at the Fermi energy.

cal results. In Ref. 96 an AF state with nearly compensating antiparallel spin and orbital moments (possibly obtained with an orbital polarization term) is proposed as a solution for the small moment antiferromagnetic (SMAF) phase but the SMAF phase is nowadays considered to be parasitic rather than intrinsic.⁴⁴

3. Density of states

The computed total and partial densities of states (DOSs) of URu_2Si_2 are shown in Fig. 8. Note that the Fermi level (at 0 eV) falls precisely in a sharp minimum of the total DOS. The contribution of the uranium $5f$ states increases, starting from about 2 eV below E_F ; at E_F and up to 1.5 eV above E_F , the uranium $5f$ dominate the DOS. The hybridized Ru $4d$ states extend from -6 to 3 eV; the hybridized Si $3p$ states extend over the same energy interval. Yang *et al.*⁶³ performed a photoemission study of URu_2Si_2 in which they employed both He I and He II radiation to locate the energy position of the $5f$'s relative to the Fermi level. From the difference of the He II and He I emission spectra Yang *et al.* inferred that the U $5f$ states are relatively delocalized and energetically extend from 1.5 eV binding energy up to the Fermi energy, where they assume a maximal contribution. The Ru $4d$ states were found to be located at about 2 eV binding energy. The computed LSDA DOS is in good agreement with these findings. Figure 8 furthermore illustrates that the total DOSs of the PM and LMAF phases are very similar, as expected. The difference between the PM and LMAF DOSs is largest in the $5f$ energy interval; the inset of Fig. 8 shows the total DOS of the two phases on an enlarged energy scale close to E_F . Due to the gap opening on a part of the FS in the LMAF phase, the DOS minimum at E_F deepens.

4. Magnetic moments

The total magnetic moment on the uranium atoms in the LMAF phase is reported to be $0.40 \mu_B$ in recent measurements.¹² Our *ab initio* calculations give a total mo-

ment of $0.39 \mu_B$, in good agreement. We note first, with regard to the value of the moment, that we observed in the calculations a sensitivity of the moment to the a and c lattice constants. For an elongated unit cell with the same volume as the equilibrium volume, but a smaller a and larger c lattice parameter, the moment increases significantly. Conversely, for a compressed equal-volume unit cell with larger a and smaller c the computed moment is slightly reduced. Such behavior has been clearly observed in uniaxial pressure experiments.⁹⁷ Second, the computed equilibrium spin and orbital moments are $M_S = 0.36 \mu_B$ and $M_L = -0.75 \mu_B$, respectively, i.e., the orbital moment is antiparallel to the spin moment and twice as large. Detailed measurements of the separate spin and orbital moments have not been reported. Nonetheless, it can be inferred that the computed spin and orbital moments separately are in good agreement with experiment. Recent neutron form factor measurements⁹⁸ indicated a value for $C_2 = M_L / (M_L + M_S)$ of about 1.8 ± 0.2 . From the theoretical values of M_L and M_S we obtain $C_2 = 1.9$, implying that the predicted values for the spin and orbital moments are indeed consistent with experiment (which, recalculating from C_2 and the total moment, gives $M_S = 0.32 \pm 0.04 \mu_B$ and $M_L = -0.72 \pm 0.08 \mu_B$).

5. Transport properties

The thermal and charge transport properties of URu_2Si_2 are experimentally well documented.^{7,9,10,30,31,34,46,99–104} The normal^{7,9,34,105} and Hall^{10,46,99,106} resistivities as well as the thermal conductivity and Nernst effect^{46,101,102} display a clear signature of the HO transition, consistent with the sudden removal of a part of the FS at T_0 . This distinct jump in the transport quantities is present both at the phase transition from the PM to the HO phase and that of the PM to the LMAF phase,^{30,34,103} yet detailed charge transport measurements revealed that the FS gapping in the LMAF phase is distinctly larger than in the HO phase.^{30,34,35,103,104} Maple *et al.*⁹ expressed the FS removal in terms of the opening of a partial FS gap Δ . The gap opening in the HO phase was measured to be about 70–80 % of that of the LMAF phase ($\Delta_{\text{HO}} \approx 75$ K and $\Delta_{\text{LMAF}} \approx 100$ K).^{34,35,103,104}

The resistivity change in the transition from the PM to the LMAF phase is accessible from the electronic structures. To compute the electrical conductivities in these two phases, we have used the Kubo linear-response formulation in constant relaxation time approximation. Apart from the Fermi velocities, the conductivity expression contains an unknown electron lifetime which enters as a constant prefactor. The electron relaxation time dependence drops out when the resistivity change is evaluated. For the DFT-GGA electronic structure we compute an unexpectedly large and also anisotropic resistivity change due to the opening of the gap at the PM to LMAF phase transition. The computed resistivity jumps are $(\rho_{\text{LMAF}} - \rho_{\text{PM}}) / \rho_{\text{PM}}(J||c) = 620\%$, and $(\rho_{\text{LMAF}} - \rho_{\text{PM}}) / \rho_{\text{PM}}(J||a) = 160\%$. In the experiments^{100,107,108} the resistivity signal is superimposed on a large background, $\sim \rho_0 + AT^2$, due to incoherent and phonon scattering. We have subtracted this background to obtain the resistivity change due to the partial FS gapping only. In this way we obtain the measured resistivity changes in the PM to HO phase transi-

tion, which are about 400% and 100% for current along the c and a axes, respectively.¹⁰⁷ These values are consistent with the resistivity jumps computed for the LMAF phase but they are somewhat smaller. This might be related to the fact that the measured resistivity jump pertains to the HO phase, in which the partial FS gap is smaller, about 70%–80 % of that of the LMAF phase.^{30,34,103} Hence, the estimated experimental resistivity changes in the PM to LMAF transition would be higher (a plain scaling would give 500% and 125% for $J||c$ and $J||a$, respectively). We also mention that the conductivity calculations pertain to the $T=0$ K coherent electronic structure, whereas the measurements were performed in the temperature range around T_0 . The observed anisotropy ratio of the resistivity jump is 4:1 (Ref. 107), a value which is in very good agreement with the theoretical anisotropy ratio of 3.9:1 predicted on the basis of the DFT-GGA electronic structures.

Magnetotransport studies revealed that URu_2Si_2 is a low-carrier, electron-hole compensated metal.^{46,92,102} As was pointed out^{24,72} recently, itinerant $5f$ calculations (LDA or GGA) indeed accurately predict this feature for URu_2Si_2 . The electron and hole Fermi volumes in the PM phase cancel each other within a numerical error of 2%.⁷² The number of holes has been determined from Hall effects measurements to be $0.017 \leq n_h \leq 0.021$ per U atom in the HO phase and 0.1 per U, respectively, in the PM phase.^{46,106} We have used the computed intraband plasma frequency, $\omega_p^2 = \frac{4\pi e^2}{mV_{\text{UC}}} n$, to determine the number of carriers, n , in both the PM and LMAF phases (V_{UC} is the unit-cell volume). In contrast to the Fermi volume, the plasma frequency is a FS integral and therefore it counts only the carriers that contribute to the transport (at $T=0$ K). The computed number of holes is 0.08/U atom and 0.0185/U atom in the PM and LMAF phases, respectively, in reasonably agreement with the experimental data. The calculated values emphasize that the FS gapping in the PM to LMAF transition strongly reduces the number of carriers by a factor of 4. Hall effect measurements give that there are about five times less carriers in the HO phase than the PM phase.¹⁰⁶

The computed $5f$ itinerant (LSDA or GGA) FS gap has recently been compared to experimental values.²⁴ The FS gap at the transition to the HO phase was first determined by Maple *et al.*⁹ from specific-heat measurements. This FS gap, averaged over the whole BZ, was estimated to be $\Delta_{\text{HO}} \approx 11$ meV. Somewhat smaller gaps for the HO phase of about 7 meV were obtained from transport measurements,^{30,34,35,100,103} and a larger gap of about 10 meV was measured for the LMAF phase.^{30,34,103} The FS gap which is predicted by DFT delocalized $5f$ calculations²⁴ is strongly \mathbf{k} dependent (see Figs. 6 and 16 below). The LMAF gap Δ_{LMAF} varies from maximally 65 meV along the Γ -M (Σ) direction to 0 meV along the Γ -X (Δ) direction. The larger theoretical gap obtained in certain places in the BZ is not inconsistent with the smaller BZ-averaged gaps obtained from transport measurements. Moreover, the computed gap pertains to the coherent ($T=0$ K) electronic structure but in the experimental analysis of the transport data both a \mathbf{k} and temperature-independent gap is assumed constant from $T=0$ K to T_0 .^{9,31,99,100,103,107}

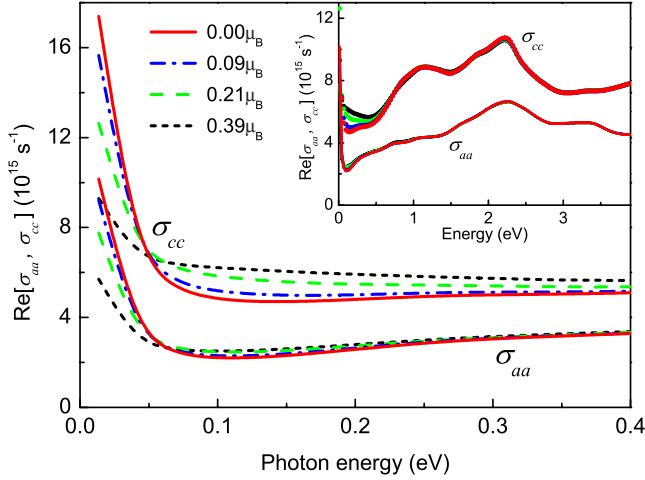


FIG. 9. (Color online) Calculated optical conductivity spectra, $\text{Re}[\sigma_{aa}(\omega)]$ and $\text{Re}[\sigma_{cc}(\omega)]$ of URu_2Si_2 . Computed spectra (at $T = 0$ K) are given for different uranium total magnetic moments, starting from that of the PM phase ($0.0 \mu_B$) up to that of the LMAF phase ($0.39 \mu_B$). The inset shows the computed spectra on a larger energy interval. Note that the $\text{Re}[\sigma_{cc}]$ spectra have been shifted upward by $3 \times 10^{15} \text{ s}^{-1}$ for sake of visibility.

6. Optical spectra

The optical spectra of URu_2Si_2 have been measured in several investigations.^{109–111} The gapping occurring in the HO phase was observed originally by Bonn *et al.*,¹⁰⁹ more detailed infrared optical measurements of the gapping with Re doping were performed by Thieme *et al.* (Ref. 110) and Degiorgi *et al.* (Ref. 111); the reported spectra^{109–111} are in good agreement with one another. A very recent optical study¹¹² obtained, however, a difference in the low-frequency response.

Using linear-response theory we have computed the optical conductivity of URu_2Si_2 for the two possible geometries, $E \parallel c$ and $E \parallel a$, where E is the electric field vector of the light. In Fig. 9 we show the calculated conductivity spectra, $\text{Re}[\sigma_{aa}(\omega)]$ and $\text{Re}[\sigma_{cc}(\omega)]$. The plotted optical conductivity spectra include both interband and intraband contributions and have been calculated for a range of static AF moments, going from the PM phase ($0.0 \mu_B$) up to the full LMAF phase ($0.39 \mu_B$). The theoretical spectra illustrate the effect of the increased opening of the FS gap in the vicinity of the Fermi energy. The optical conductivities, being maximal for the PM phase near zero energy, become progressively reduced for the various static antiferromagnetic phases, in particular, for small photon energies well below 50 meV. The largest drop of $\text{Re}[\sigma(\omega)]$ is obtained for the LMAF phase, where the FS gapping is the largest. The computed behavior agrees reasonably well with experimental observations. Bonn *et al.*¹⁰⁹ measured the optical response of URu_2Si_2 in the basal plane ($E \parallel a$). They observed a reduction in the reflectivity in the HO phase for photon energies below 30 meV. Our calculation predicts a drop in $\text{Re}[\sigma_{cc}]$ below 40 meV. Bonn *et al.* did not measure σ_{cc} ($E \parallel c$), but our calculations predict that a larger reduction should occur for $\text{Re}[\sigma_{cc}]$ at small energies well below 50 meV. We also note that to-

gether with the progressive FS gapping, there is a transfer of spectral weight to higher energies. $\text{Re}[\sigma_{aa}]$ increases slightly above 50 meV. A larger spectral weight transfer occurs for $\text{Re}[\sigma_{cc}]$ for energies of 50 up to 600 meV (see inset in Fig. 9). Above 200 meV and 600 meV, respectively, the influence of the gapping on the optical conductivity spectra for $E \parallel a$ and $E \parallel c$, respectively, has vanished.

The inset in Fig. 9 shows the computed spectra for $E \parallel a$ and $E \parallel c$ on a wider energy scale. An interband peak is presented just above 2 eV in both $\text{Re}[\sigma_{aa}]$ and $\text{Re}[\sigma_{cc}]$. Experiment also detected a peak at this energy.¹¹¹

The experimental spectra^{109,110} reveal a particular feature which is not present in the calculated spectra. The reduction in the Drude weight at low frequencies leads to an increased spectral weight at 7–8 meV.^{109,110} The origin of this transferred spectral weight is currently unknown; it was not observed in a recent study.¹¹² It might nonetheless signal a difference between the experimental and computed theoretical spectra.

7. Specific heat and magnetic entropy

The linear-temperature specific-heat coefficient of URu_2Si_2 in the HO phase is, with about 50 mJ/mol K²,^{7–9,113} not particularly high, implying that URu_2Si_2 in this phase is not a heavy-fermion material. The Sommerfeld coefficient is comparable to that of, e.g., UGa_3 ,¹¹⁴ which is an itinerant antiferromagnet.^{71,115} The unrenormalized specific-heat coefficient calculated with the LSDA approach is about 9 mJ/mol K², i.e., there is an expected mass renormalization of six, a value not unusual for actinides. As a consequence, the computed LSDA bands will become renormalized, but not strongly. Our LDA+DMFT calculations (to be presented below) indicate a further influence of the dynamic part of the electronic self-energy $\Sigma(\omega)$, through which a renormalization of the bare LSDA band masses would occur. However, as we can currently not compute $\text{Re}[d\Sigma(\omega)/d\omega]$ down to low enough temperatures, we refrain from giving values for the estimated mass renormalization. Also, low-energy spin fluctuations, which are not accounted for in the bare specific-heat coefficient, can be expected to give a considerable enhancement.⁵⁵

The entropy of URu_2Si_2 has drawn attention from the beginning.^{8,9,113} The phase transition to the HO state was originally discovered from a λ -type anomaly in the specific heat;^{7–9} the related magnetic entropy change in the λ anomaly is, with about $0.16R \ln 2$, relatively large.^{8,9,113} Such entropy removal can, in particular, not be explained¹¹⁶ by assuming a phase transition to a SMAF state that at first was thought to be connected to the HO transition.^{39–42}

The total magnetic entropy S_m has been determined by van Dijk *et al.*⁵⁵ and Janik,⁵⁴ through subtracting the measured specific heat of ThRu_2Si_2 , which has no $5f$ electrons, from that of URu_2Si_2 . From the specific-heat difference a total electronic entropy $S_m(T) = \int_0^T (\Delta C/T') dT'$ approaching $R \ln 4$ (mJ/mol K) was obtained.⁵⁴ This value is not inconsistent with our LSDA calculations, predicting a low-temperature $5f$ count of 2.7. Assuming at higher temperatures an occupancy of three $5f$ electrons, a spin entropy of $R \ln 4$ [i.e., $R \ln(2S+1)$, with $S=3 \times 1/2$] follows.

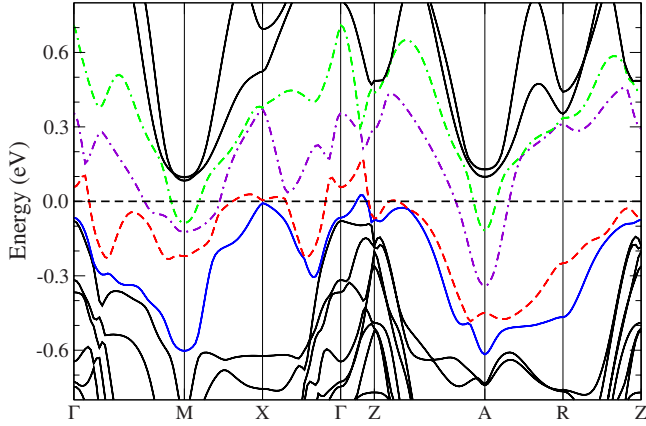


FIG. 10. (Color online) Energy dispersions of URu_2Si_2 in the LMAF phase, computed with the around mean-field GGA+ U approach, with $U=1.4$ eV and $J=0.68$ eV. The bands crossing the Fermi level are highlighted.

For the HO phase, the total electronic entropy at T_0 amounts to about $0.25R \ln 2$ (Ref. 113). As was pointed out several times, assuming the opening of a gap Δ in the electronic spectrum, the electronic specific heat would scale as $C_m(T) \propto \exp(-\Delta/k_B T)$, which fits the measured specific heat in the HO phase extremely well.^{9,55,113} In fact, the opening of gap in the magnetic excitation spectrum can *wholly* explain the entropy removed at the HO transition.^{53,55} The magnitude of the gap was estimated to be about 11 meV from specific-heat measurements,^{9,113} or smaller from inelastic neutron measurements.^{35,53,117} Our energy band calculations also show that the HO gapping removes a considerable amount of accessible states at E_F . The band-structure gap computed here is in fact larger, maximally 60 meV (for the LMAF phase) but it is strongly k dependent. The k -averaged gap would thus be considerably smaller and be consistent with the entropy loss associated with the HO transition.

B. LSDA+ U and $5f$ -core calculations

Actinide materials with enhanced Coulomb correlations between the $5f$ electrons can be computationally treated with LSDA+ U or GGA+ U calculations (see, e.g., Refs. 118–120), which are expected to give a good description for materials with a moderate degree of $5f$ localization. Actinide or lanthanide materials with localized f electrons are conversely well described by open f -core calculations in which the f 's are treated as unhybridized core electrons (see, e.g., Ref. 121).

The energy bands of AF URu_2Si_2 computed with the “around-mean-field” GGA+ U approach are shown in Fig. 10. For the Coulomb U and exchange J parameters we have chosen the values $U=1.4$ eV and $J=0.68$ eV. The U value can be considered as relatively small and has been chosen such in order not to depart much from the LSDA solution. Nonetheless, the computed bands in Fig. 10 reveal that the bands near the Fermi level are modified to a considerable extent so that also the FS becomes quite different. The bands near the M point are pushed down, whereby new FS sheets appear. Bands near the X and Γ points are pushed upward,

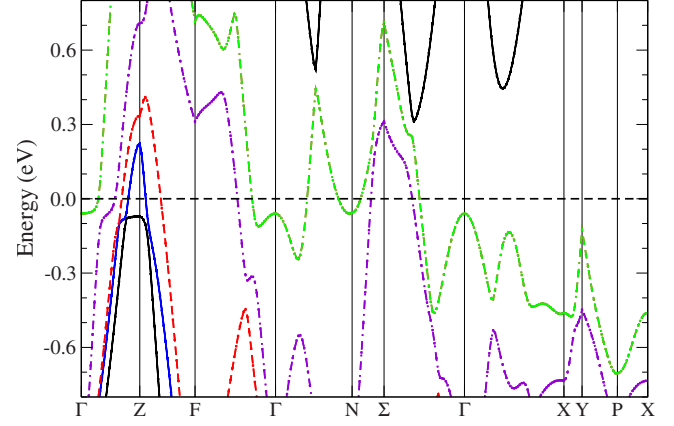


FIG. 11. (Color online) Energy dispersions of nonmagnetic URu_2Si_2 computed with a localized $5f^2$ configuration. The highlighted bands are the ones crossing the Fermi level. The used high-symmetry points in the bct BZ are indicated in Fig. 1.

whereby also a new FS sheet appears around X. Furthermore, two new electron pockets appear around A. The gap features along the Γ -M and Γ -X directions are strongly affected; the gapping occurring along Γ -M has practically vanished. As we shall see below, experiments support in fact the Fermi surface predicted by LSDA calculations. This illustrates that the Fermi surface and its gapping is rather sensitive to the Coulomb U in GGA+ U calculations. This is understandable, as the FS gap is quite small (several tens of millielectron volt) and the opening of the FS gap is due to a subtle hybridization change in $5f$ bands just above and below the Fermi level. The Coulomb U acting on the $5f$ states changes the $5f$ band dispersions substantially.

As mentioned before, a large number of theories for the HO of URu_2Si_2 are based on the assumption of completely or nearly localized $5f$ electrons.^{14,16,19,21,23,26,28,50–52} Particularly, an underlying localized $5f^2$ configuration has been discussed recently.^{19,21,23,26,28,52} In itself, a localized $5f^2$ configuration possesses very interesting properties, as it can sustain both a nonmagnetic spin-singlet and a magnetic triplet configuration, something which might be related to the occurrence of two different phases.

In Fig. 11 we show the energy dispersion computed for paramagnetic URu_2Si_2 with the open-core approach for a localized $5f^2$ configuration. As expected, the f -core energy bands are very different from the bands obtained for PM URu_2Si_2 assuming itinerant $5f$ valence states. Such band structure of URu_2Si_2 , computed with WIEN2K in the PM phase was reported already in Ref. 72 and is therefore not repeated here. The f core energy dispersions are indeed so different from the $5f$ delocalized ones that it makes no sense to compare them. As mentioned before, the $5f$ occupancy obtained from LSDA itinerant $5f$ calculations is about 2.7. Even with a dependence on the used muffin-tin sphere radius, this occupation number is not two. Hence, it is understandable that very distinct energy dispersions emerge. The concomitant FS's are consequently also very different, as will be exemplified below when we discuss the FS of URu_2Si_2 in detail.

LSDA- $5f^2$ core calculations were recently also performed by Haule and Kotliar,²⁶ who only show a small reciprocal

space section of the bands in a narrow energy interval near the Fermi level and around the Γ point, yet their results agree with our full-potential results. In particular, there is one band at the Γ point near E_F that has an inverted parabolic shape, and there are two bands with a steep dispersion crossing the Fermi level between Γ and Σ .

Whether or not a localized $5f^2$ picture is more appropriate for URu_2Si_2 has to be considered in the light of all available experimental data. The delocalized $5f$ picture provides a quite accurate description of the known experimental data; this cannot be said of the localized $5f^2$ configuration. In first instance one might think that the LMAF phase might be related to a magnetic, localized $5f$ configuration, but the delocalized $5f$ approach is thus far the only one that has provided an accurate explanation of the LMAF phase, which is a conventional antiferromagnetically ordered state without mysterious properties.

C. DMFT calculations

In our LDA+DMFT calculations we used a large number of Matsubara frequency points (8192) when taking the sum over the frequencies on the temperature axis, nonetheless, we can only compute a finite number of frequency points and therefore the calculations are valid for moderately high temperatures in practice (100 K and above). This implies that we can investigate the influence of dynamical electron configuration fluctuations in the paramagnetic phase. At high temperatures the uranium $5f$ moments are expected to behave as incoherent, local moments. Note that the single-ion Kondo temperature is estimated to be 370 K in URu_2Si_2 .¹⁰ With reducing temperature, lattice coherence between the f moments develops below 100 K, leading to a coherence temperature T^* of about 70 K, which is witnessed by a maximum in the normal and Hall resistivities.^{7,10} Below the coherence temperature T^* the $5f$ local magnetic moments are incorporated into the conduction electron sea, which greatly enhances the electron effective masses and, for conventional Kondo lattice materials, is expected to enlarge the Fermi surface, too.

In the LDA+DMFT calculations we started from computed LDA Kohn-Sham states that are subsequently used in the DMFT self-consistency loop. In the DMFT part we assumed effective U values of 0.4 and 0.6 eV (in both cases, J was set to 0.0 eV). These U values are chosen to approximate the more localized behavior of the $5f$'s that is anticipated at higher temperatures.

In Fig. 12 we show the computed quasiparticle density of states of URu_2Si_2 for several temperatures. Pronounced changes in the quasiparticle DOS occur around the chemical potential (at 0 eV). Lowering of the temperature and increase in electron coherence leads to the typical opening of a quasiparticle coherence gap (also called hybridization gap) of about 100 meV. Concomitant with the opening of the quasiparticle gap, there is a buildup of spectral weight on both sides of the gap. The development of coherence gaps has been observed with infrared optical spectroscopy for several f -electron materials¹²² but for URu_2Si_2 this property has not yet been reported.

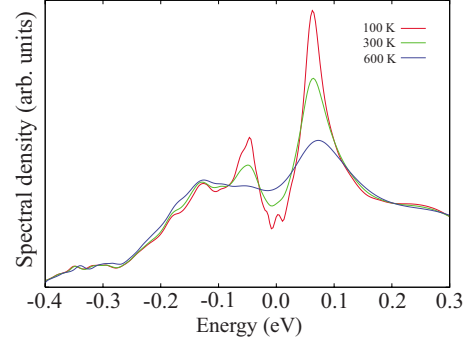


FIG. 12. (Color online) The k -integrated quasiparticle DOS calculated with the LDA+DMFT approach for URu_2Si_2 in the high-temperature, nonmagnetic phase.

In Fig. 13 we show the calculated quasiparticle bands of URu_2Si_2 at $T=100$ K. The bright colors depict a high intensity of the spectral function. For comparison, the nonmagnetic LDA bands are shown by the black lines. Note that the Z' point on the reciprocal space abscissa is positioned in the neighboring BZ. We observe that the LDA+DMFT quasiparticle bands are relatively close to the LDA bands. Their similarity is even more so for energy bands below -1 eV (not shown here) because these bands possess less uranium f character. Some differences between the LDA and quasiparticle bands can nonetheless be seen from Fig. 13. In the N-P-X panel the quasiparticle band just above E_F moves distinctly closer to E_F and becomes flatter. Near the X point the quasiparticle band below the Fermi level moves slightly upward and disperses stronger downward toward the Γ point. The k -dependent quasiparticle DOS gives the impression of a band dispersing downward from above the X point toward the Γ point and crossing E_F between the two points.

Another DMFT calculation for URu_2Si_2 has been reported recently by Haule and Kotliar.²⁶ We note that our DMFT results are distinctly different from those of Ref. 26. We have performed DMFT calculations using the spin-polarized FLEX impurity solver, starting from LDA results, which should be valid for the weakly correlated uranium f electrons at higher temperatures. The DMFT calculations of Ref. 26, on the other hand, used the one-crossing approximation solver together with a nearly localized uranium $5f^2$ configuration. The difference can be understood to arise from the $5f$ configuration used in the LDA or LDA+ U band-structure

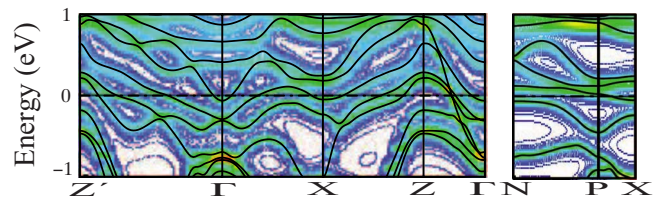


FIG. 13. (Color online) The LDA+DMFT quasiparticle bands of URu_2Si_2 at $T=100$ K (for details, see text). Bright colors indicate a high intensity of the k -dependent spectral function, $-\frac{1}{\pi}\text{Im } G(\mathbf{k}, E)$. Black lines show the LDA energy bands for comparison. Note that Z' denotes the Z point in the neighboring bct Brillouin zone.

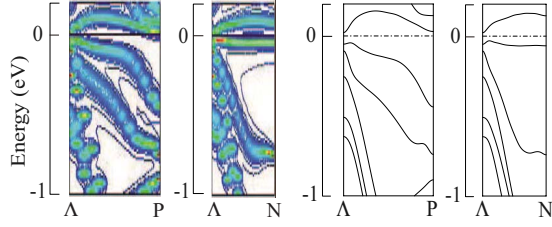


FIG. 14. (Color online) Left: LDA+DMFT quasiparticle bands for the directions Λ -N and Λ -P in the bct BZ ($\Lambda=Z/2$). Bright colors denote a high intensity of the k -dependent spectral function. Right: the LDA energy bands for the same directions.

part of the LDA+DMFT calculation, which obviously determines largely the gross electronic structure, whereas the DMFT part involving dynamical self-energy fluctuations induces mainly modifications of energy dispersions in the vicinity of the chemical potential.

DMFT k -dependent spectral functions can be compared to ARPES data. Several ARPES measurements on URu_2Si_2 have been reported.^{65–67} Ito *et al.*⁶⁵ and Santander-Syro *et al.*⁶⁷ both used a He I light source, whereas Denlinger *et al.*⁶⁶ used tunable synchrotron radiation. Only the recent experiment of Santander-Syro *et al.* measured quasiparticle bands below T_0 . These latest measurements indicate the existence of a narrow band just below E_F in the HO phase, as well as of an inverted parabolic band at $k=0$ below E_F ; the latter band was attributed to a surface state.⁶⁷ In our $5f$ -itinerant LSDA calculation there is no such inverted parabolic band at the Γ point, but LDA localized $5f^2$ electron calculations do predict such a band (see Fig. 11), as do also the recent LDA+DMFT calculations of Haule and Kotliar.²⁶ As photoemission at this energy is very surface sensitive, it could thus be that this band stems from a $5f$ -localized response of uranium atoms on the surface. Further investigations are therefore needed to definitely establish the origin of the inverse parabolic band. A bulk, flat band just below E_F at the Γ point is not predicted by our delocalized $5f$ LDA or LDA+DMFT calculations. We note, however, first, that the LDA and LDA+DMFT bands have a significant dispersion along the k_z direction and second, that the k_z position in the BZ will, in a normal-emission ARPES experiment, depend on the energy of the used radiation. With He I radiation, a k_z position between Γ and Z in the bct BZ will be probed,⁶⁵ probably being closer to Γ than Z . In Fig. 14 we present computed LDA and LDA+DMFT bands for the midpoint, $\Lambda=Z/2$, between Γ and Z , and going to the P and N, respectively, high-symmetry points in the bct BZ (see Fig. 1). The plotted bands illustrate that a flat band exists in the P- Λ -N plane, just below E_F , being mostly flat near $k_x, k_y=0$. At this point it is still too early to decide whether this computed flat band does or does not correspond to the observed ARPES structure.⁶⁷ High-resolution ARPES measurements with tunable photon energy will be required to reveal the full electronic dispersions in the HO phase.

D. Fermi surface of URu_2Si_2

1. Nesting vectors

An appropriate description of the Fermi-surface topology of URu_2Si_2 is an indispensable ingredient for unraveling the

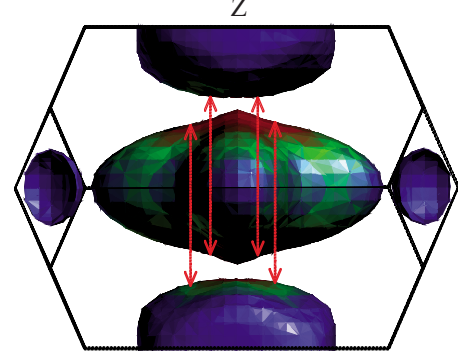


FIG. 15. (Color online) Side view of the Fermi surface of PM URu_2Si_2 along the k_x or k_y axis of the bct BZ (see Fig. 1). The arrows indicate the AF nesting vector (with length $2\pi/c$) connecting the two FS sheets. Note that two smaller FS sheets (one Z -centered ellipsoid and one small Γ -centered ellipsoid) are not seen here.

nature of the HO phase as well as the unconventional SC.^{46–48,106} Experimental information regarding the FS of URu_2Si_2 has been gained from nesting vectors, identified through inelastic neutron experiments,^{38,42,53,123} and through extremal FS orbits, obtained from quantum-oscillation experiments.^{36,92,105}

To start our discussion, we show a side view of the FS of PM URu_2Si_2 , computed with the LSDA approach, in Fig. 15. The two FS sheets reveal the existence of a nesting vector with length $c^*=2\pi/c$ (i.e., half the distance from one Γ point to the next-nearest Γ point). These two FS sheets have a similar round curvature, favorable for nesting, with the exception that close to $Z/2$ the Γ -centered sheet has a more pointed part, with only a small area that would not be favorable for nesting. This FS part corresponds to a small part at the Z point in the simple tetragonal cell, which we believe to be insignificant.²⁴ The identified nesting vector fits accurately to the antiferromagnetic wave vector $\mathbf{Q}_{\text{AF}}=(0,0,1)$ of longitudinal spin fluctuations observed in the HO phase with inelastic neutron-scattering experiments,^{38,39,53} and it is the AF ordering vector of the LMAF phase.^{38,42} This nesting vector is important for understanding the low-temperature behavior of URu_2Si_2 . When a coherent state emerges at temperatures sufficiently below the coherence temperature T^* , the system develops a FS sustaining this nesting vector, which is favorable for AF spin fluctuations in the HO phase and formation of long-range AF order in the LMAF phase. Inelastic neutron experiments³⁸ showed that the inelastic response at \mathbf{Q}_{AF} in the HO phase becomes the static AF Bragg peak of the LMAF phase.³⁸ The thereby induced symmetry breaking implies a folding of the bct BZ at $Z/2$, i.e., folding Z to Γ .

A second, incommensurate nesting vector of URu_2Si_2 has been detected at $\mathbf{Q}_1=(1\pm 0.4,0,0)$.^{38,42,53} This nesting vector has been observed in *both* the HO and LMAF phases.³⁸ In Fig. 16 we show a cross section of the LMAF and PM Fermi surfaces in the $z=0$ plane. To draw comparison, both FS cross sections are plotted in the simple tetragonal unit cell of the LMAF phase. As was reported recently,²⁴ a clear nesting occurs (depicted by the dashed arrow) at $0.4a^*$ ($a^*=2\pi/a$),

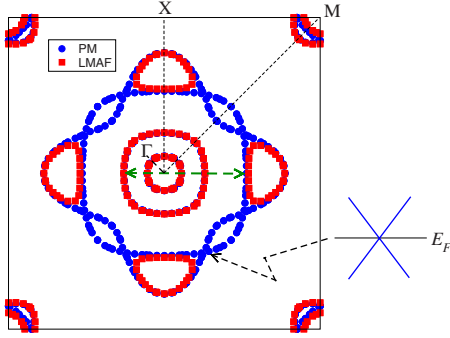


FIG. 16. (Color online) Cross sections of the PM (circles) and LMAF (squares) Fermi surface in the $z=0$ plane of the simple tetragonal BZ. The Fermi-surface portions along the Γ -M directions are gapped in the PM to LMAF transition. Note that other Fermi-surface parts are completely unaffected; the LMAF Fermi-surface cross sections are on top of the PM ones. The thick dashed arrow indicates the nesting vector $0.4a^*$, the thin dashed arrow indicates the position of one of the eight degenerate band crossings precisely at the Fermi energy E_F .

implying a nesting vector that matches precisely the measured incommensurate vector $\mathbf{Q}_1 = (1 \pm 0.4, 0, 0)$. Figure 16 illustrates that \mathbf{Q}_1 is a suitable nesting vector for the LMAF phase, but less so for the PM phase (shown by blue circles), because in the latter phase the FS curvature does not support nesting as much. Hence, the incommensurate nesting vector is characteristic for the LMAF phase but not for the PM phase. *A priori* we do not know how the FS in the HO phase looks like, because this would require knowing the order parameter of the HO, but it is known that de Haas-van Alphen experiments could not detect any notable difference between the FSs of the HO and LMAF phases.³⁷ Likewise, inelastic neutron-scattering experiments³⁸ give the same incommensurate wave vector in the HO and LMAF phases. From these facts we infer that the FS of URu_2Si_2 in the HO phase should be quite close to the one we have computed for the LMAF phase.

Figure 16 in addition illustrates the positions of the FS hot spots in the $z=0$ plane. The degenerate crossing of two bands occurs right at E_F at eight places, indicated by the thin dashed arrow. At these hot spots there exists an instability of the FS as a small perturbation may already cause a lifting of the degeneracy and hence cause a topological FS reconstruction (Lifshitz transition).

The gap symmetry in the superconducting phase has been discussed recently^{46–48} but the symmetry of the partial gap in the HO phase has not yet been studied. The calculations in Fig. 16 illustrate that the HO gap has in the $z=0$ plane a fourfold symmetry, in which there exist nodal lines with $d_{x^2-y^2}$ symmetry in the ST structure, which is equivalent to nodal d_{xy} symmetry in the bct structure. A possible additional phase factor in the gap structure might exist but cannot be deduced from the current calculations.

2. Quantum oscillations

Details of the FS of URu_2Si_2 has been investigated, too, through studies of quantum oscillations in dHvA and

TABLE I. Comparison of experimental and *ab initio* calculated extremal FS areas in URu_2Si_2 for $H \parallel c$. The FS cross-sectional areas are labeled according to the convention of Refs. 92 and 105 and have been determined with de Haas-van Alphen (dHvA) measurements (Ref. 92) or Shubnikov-de Haas (SdH) measurements (Refs. 36 and 105). The theoretical FS orbits are shown in Fig. 17. All FS cross-sectional areas are given in kT.

Orbit	dHvA (Ref. 92)	SdH (Ref. 105)	SdH (Ref. 36)	Calc.
ε		1.35		1.37
α	1.05	0.98	0.85	0.76
β	0.42	0.50	0.48	0.48
γ, γ'	0.19	0.25	0.22	0.26

Shubnikov-de Haas (SdH) measurements.^{36,92,105,124–126} In earlier experiments,^{124–126} only a few extremal orbits could be detected. The more recent dHvA and SdH measurements^{36,92,105} on purer crystals have provided a consistent set of data for the quantum oscillations in URu_2Si_2 . These experimental data are listed together with the calculated extremal FS cross-sectional areas in Table I. The dHvA experiments of Ohkuni *et al.*⁹² as well as the SdH experiments of Jo *et al.*³⁶ revealed three FS orbits, which these authors labeled α , β , and γ . However, it was already noted⁹² that one or more orbits were missing because the cyclotron mass of the small FS orbits would not be able to account for the full, enhanced mass that was deduced from the specific heat. Quite recently, it was shown with SdH experiments on ultraclean crystals¹⁰⁵ that there is indeed a further branch, which was named the ε branch. The calculated FS of URu_2Si_2 is shown in Fig. 17, where we have also indicated the theoretical extremal orbits ε , α , β , and γ for magnetic field along the z axis. Note that there is a small Γ -centered ellipsoid (γ') which is not visible in Fig. 17 because it is masked by the large Γ -centered ellipsoid. Table I illustrates that the calculated extremal orbits of the four branches are in quite good agreement with the available experiments. The computed orbits pertain to the LMAF phase, however, consistent with the observations made above, we assume the same FS for the HO and LMAF phases. The newly discovered¹⁰⁵ ε branch corresponds to the large Γ -centered rugby ball, stemming from band 107 in our calculations. The earlier reported extremal orbits correspond to the M-centered ellipsoids (branches α and γ , band nos. 109 and 111), the rounded half sphere (β , band no. 109), and the small, Γ -centered sphere (γ' , band no. 107). The computed frequencies of these extremal orbits agree well with dHvA and SdH measurements: the extremal areas of the ε and β orbits are well reproduced. The α orbit is somewhat smaller than the experimental value and the γ orbit is somewhat larger. The calculations predict, in fact, a γ and a γ' orbit, which have nearly the same frequency. Also, as discussed below, the angular dependence of their cross-sectional area is very similar. This similarity appears to be coincidental. Experimentally, it would thus be difficult to distinguish between the γ and γ' branches. One other difference between the experiments and the calculations is that the calculations predict an additional, small FS part around the Z point (see Fig. 17). Its

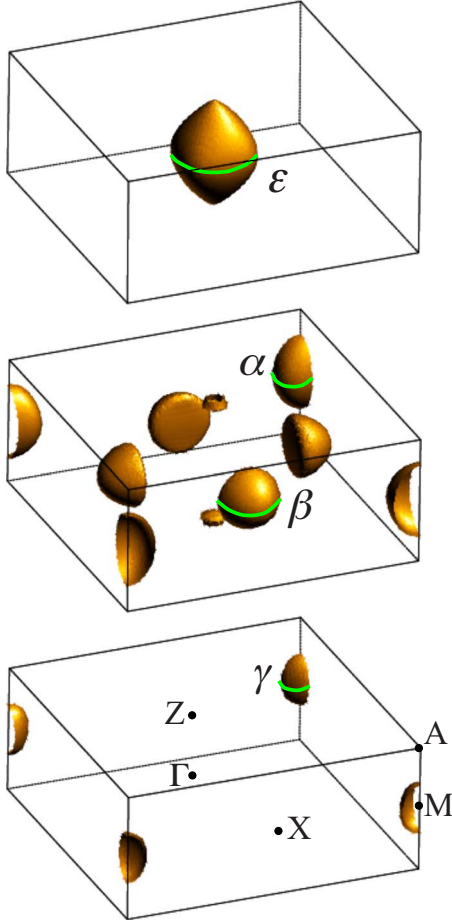


FIG. 17. (Color online) Computed Fermi-surface sheets of URu_2Si_2 in the LMAF phase. The extremal Fermi-surface orbits for field along the z axis are indicated. Not shown is the small Γ -centered ellipsoid (γ') that is inside the large Γ -centered surface in the top panel. High-symmetry points are indicated in the bottom panel.

extremal area is very small (about 0.07 kT) and, as mentioned previously,²⁴ its occurrence is related to an insignificant, small FS area at the Z point which occurs through band folding. The origin of this small FS sheet is the pointed part of one FS sheet near $\pm Z/2$ in the PM phase (Fig. 15), which causes an imperfect nesting of the two FS sheets and hence an incomplete FS gapping near the ST Z point when being folded to the LMAF phase.

We briefly mention that earlier studies of quantum oscillations in URu_2Si_2 were reported by Bergemann *et al.*,¹²⁴ Ohkuni *et al.*,¹²⁵ and Keller *et al.*¹²⁶ Although the measurements were performed on less well-defined samples, there are some consistencies with the newer data. Bergemann *et al.* report the observation of two orbits, which cross-sectional areas of 1.09 and 0.41 kT for magnetic field along the c axis. Keller *et al.* reported magnetoresistive measurements from which they obtained several SdH frequencies of about 1.0 and 0.2 kT.

The crystallographic anisotropy of the extremal FS areas has been investigated by angular-dependent dHvA and SdH experiments. The computed angular dependence of the FS areas is shown in Fig. 18, for field directions in the bct cell.

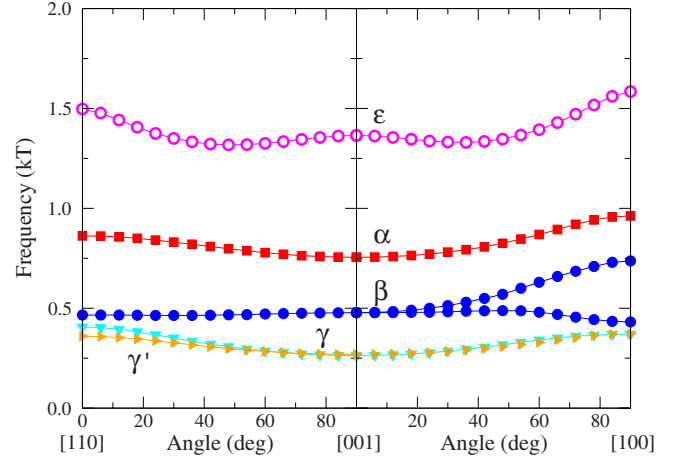


FIG. 18. (Color online) Calculated dependence of the extremal FS cross sections of URu_2Si_2 on the magnetic field direction. The extremal orbits are visualized in Fig. 17.

A comparison of the computed angular dependence with experimental data reveals a good overall correspondence. Ohkuni *et al.*⁹² report that the α , β , and γ branches are quite flat, i.e., corresponding to nearly spherical FS sheets. Shishido *et al.*¹⁰⁵ also report that the α and β branches are flat and due to spherical FSs. As Fig. 18 shows, the theoretical FS sheets are predicted to be relatively spherical, and hence, a very similar angular behavior is furnished by the calculations. Moreover, a more detailed comparison reveals that the angular anisotropy of the ϵ , α , and β branches is also in good agreement with experiment. The extremal frequency of the α orbit is predicted to increase from the $[001]$ to $[100]$ direction, which was also found experimentally.⁹² The frequency of one part of the β orbit decreases slightly, in accordance with experiment. The four half spheres in the $z=0$ plane are anisotropic with respect to the field direction, therefore the single β orbit for field $H\parallel c$ splits in two orbits for fields along $[100]$ but no splitting occurs along $[110]$. Such a splitting of the β branch has been detected recently in SdH experiments.¹²⁷ The ϵ orbit increases in the $[100]$ direction, which was also observed in recent SdH measurements.¹⁰⁵ However, the SdH experiment¹⁰⁵ finds a larger increase than the theory predicts.

The crystallographic anisotropy calculated for the γ orbit is not in accordance with experiment; the calculation predicts a slight increase in the frequency for magnetic fields toward $[100]$ but the dHvA experiment⁹² observed a slight decrease. Ohkuni *et al.*⁹² mention, however, that the signal of this orbit is very weak and therefore it was difficult to follow the orbit under angular field variation. The recent SdH experiments¹⁰⁵ could not determine the angular dependence of the γ orbit for the same reason. We also note, lastly, that the difference between the γ and γ' extremal orbits is predicted to be larger for fields along the $[110]$ direction.

As a nearly localized uranium $5f^2$ configuration has been suggested to be applicable to URu_2Si_2 ,^{26,28} we briefly consider the FS that would correspond to such configuration. In Fig. 19 we show the FS computed for URu_2Si_2 in the LMAF phase obtained for a localized $5f^2$ configuration. Obviously, this FS is much larger than that computed assuming delocal-

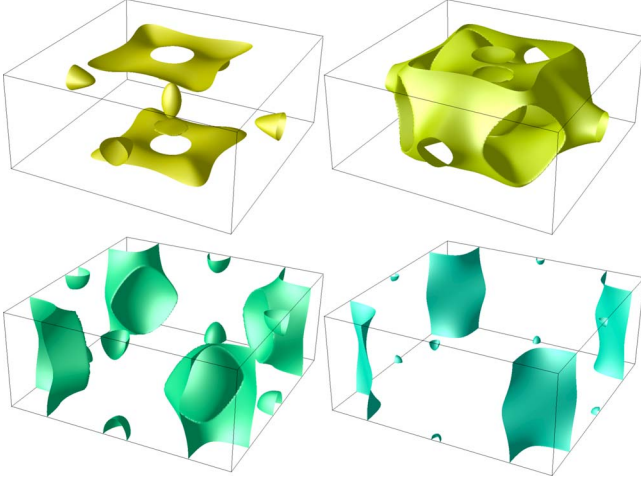


FIG. 19. (Color online) The Fermi surface of URu_2Si_2 in the LMAF phase computed with a $5f^2$ local uranium configuration.

ized $5f$'s.¹²⁸ In addition, there are quite a number of extremal orbits (more than ten for $H\parallel z$). Both these aspects of the $5f^2$ localized FS are not in correspondence with experiments. We have in addition computed the FS corresponding to a $5f^3$ localized configuration; the resulting FS is shown in Fig. 20. For the localized $5f^3$ uranium configuration the FS exists of several open FS sheets, leading to many extremal orbits. Also, several FS sheets have a cylindrical shape, in contrast to the small, closed FS pockets detected in experiments. Hence, we observe neither for the local $5f^2$ FS nor for the local $5f^3$ FS a correspondence with experiment. Conversely, the overall agreement between the experimental and theoretical FSs computed with delocalized $5f$'s can be regarded as quite good, a result which definitely supports that the theoretically predicted LSDA/GGA FS is in close agreement with the experimental Fermi surface.

E. Longitudinal spin fluctuations and dynamical symmetry breaking

1. Potential relevance of AF spin fluctuations

A significant difference between the HO and LMAF phase is the existence of an intense mode of long-lived longitudinal AF fluctuations at the wave vector \mathbf{Q}_{AF} in the HO phase, which has been identified as a fingerprint of the HO.^{35,38} This AF mode was studied in inelastic neutron experiments by Broholm *et al.*,^{39,42} Wiebe *et al.*,⁵³ and Villaume *et al.*,³⁸ and in x-ray scattering experiments by Bernhoeft *et al.*^{129,130} The longitudinal fluctuation was estimated^{39,43} to amount to $\Delta M_z \propto 1.2 \mu_B$, its characteristic time scale is on the order of picoseconds or slower.³⁵ The potential importance of the longitudinal AF mode for the HO phase was recently emphasized by Elgazzar *et al.*²⁴

Although the existence of the intense AF mode in the HO phase is evident, its connection to the HO phase is not yet fully understood. A major question in the discussion is whether a mode of long-lived AF fluctuations can induce any FS gapping. In ordinary materials, a mode of (normally transversal) spin excitations would be a very weak perturba-

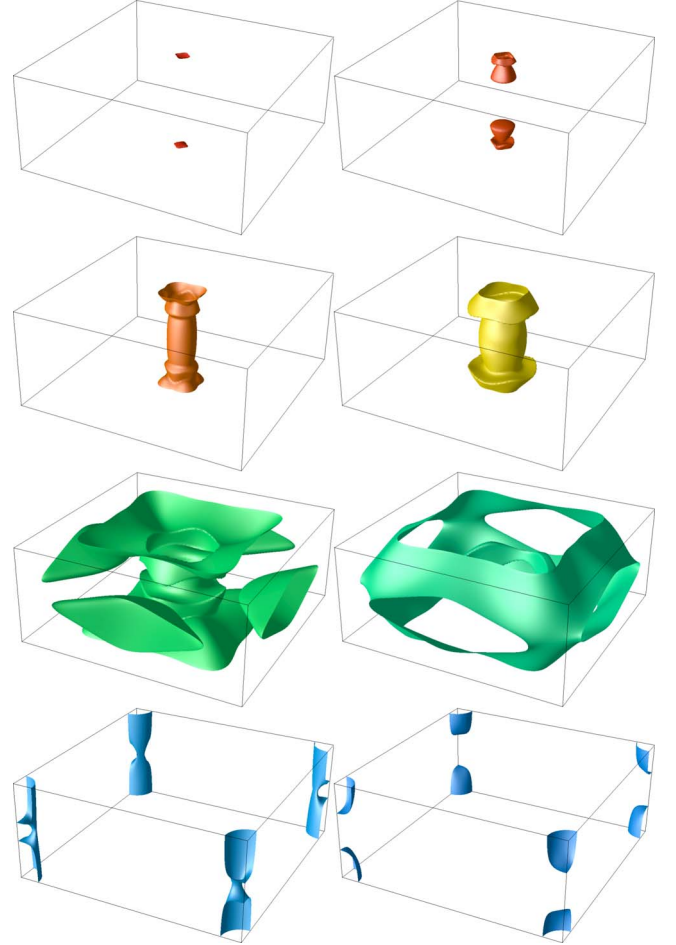


FIG. 20. (Color online) The Fermi surface of URu_2Si_2 in the LMAF phase computed with a $5f^3$ local uranium configuration.

tion of the electronic structure, and hence it cannot produce any significant transition in the bulk thermodynamic or transport properties. However, URu_2Si_2 is an exceptional material, as we find that a substantial FS gapping of 750 K occurs through symmetry breaking on an energy scale of less than 7 K. To investigate the influence of the inelastic mode we consider the fluctuating longitudinal magnetic moment on one of the two uranium sublattices, i.e., $M_z(t) \approx M_0 \cdot \cos(\omega t)$. M_0 is the maximal amplitude of the longitudinal mode which we assume to be the same as the static LMAF moment of $0.39 \mu_B$. We furthermore assume for simplicity a dispersionless frequency $\omega(q) \approx \omega$. This is a good approximation near \mathbf{Q}_{AF} . Obviously, the resulting average sublattice moment, i.e., averaged over a sufficiently long time scale τ , $\bar{M}_z = \tau^{-1} \int M_z(t) dt$, will vanish.

Next we consider what happens to the FS hot spots due to the presence of the longitudinal mode. At discrete time steps we can treat the AF mode as a frozen static antiferromagnetic arrangement with a certain amplitude of the moment M_z . At each time snapshot, the static AF arrangement will affect the FS hot spots, such that the degeneracy of bands at the Dirac points will be lifted. As the degeneracy at the Dirac points is quite sensitive, already for small static AF moments a FS gapping appears. In Fig. 21 we plot the size of the FS gap as a function of the static AF moment. The gapping appears for

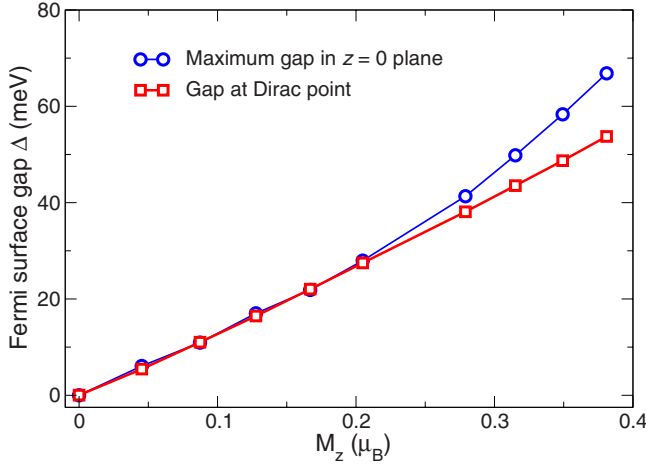


FIG. 21. (Color online) Size of the FS gap of URu_2Si_2 in the $z=0$ plane, computed as a function of the amplitude of the static AF uranium moment along the c axis.

small AF moments only at the FS hot spots but for increasing moments the gap widens until the hole FS part centered along the Γ -M direction has been gapped (cf. Fig. 16). The magnitude of the computed gap develops, to a reasonable approximation, as a linear function of M_z .²⁴ Figure 21 additionally shows that the maximal FS gapping shifts from being at the hot spots for moderate M_z amplitudes to being along the Γ -M axis for the largest amplitude. For the time dependence of the gap caused by moderately slow spin fluctuations it is essential to note that the gap Δ is an even function of M_z . Using that the magnitude of the calculated gap is a linear function of the moment M_z , we can write $\Delta(t) = \alpha |M_z(t)|$, with α a positive constant. The time dependence of the moment gives the time dependence of the gap, $\Delta(t) = \Delta_0 |\cos(\omega t)|$, with $\Delta_0 = \Delta_{\text{LMAF}}$, the maximal gap occurring for the LMAF phase. The time-averaged, macroscopic gap $\bar{\Delta}_{\text{HO}}$ follows from

$$\bar{\Delta}_{\text{HO}} = \frac{1}{\tau} \int \Delta(t) dt = \frac{\Delta_0}{\tau} \int |\cos(\omega t)| dt = \frac{2}{\pi} \Delta_{\text{LMAF}}. \quad (1)$$

Hence, with these approximations we estimate that the time-averaged HO gap is 64% of the gap of the LMAF phase. This value is in reasonable agreement with experimental data obtained from resistivity measurements that find that the HO gap is 70–80 % of that of the LMAF phase.^{30,34,103,104}

Consequently, in the special case of URu_2Si_2 a long-lived AF mode can indeed induce a substantial FS gapping. Moreover, the similarity detected experimentally in the FS gapping of the HO and LMAF phases can be explained by the presence of the AF mode in the HO phase and AF order in the LMAF phase. Nonetheless, in spite of the similar gapping, thermodynamic and transport properties, we emphasize that the HO and LMAF are distinct phases. In the LMAF phase the sublattice U moment M_0 is nonzero and thus is the standard OP for an ordered AF material. In the HO phase, conversely, $\bar{M}_z = 0$ and can obviously not be a suitable order parameter for the HO. We note that in the here-developed theory it is the amplitude $M_0(T)$ of the longitudinal AF mode

that determines the magnitude of the time-varying gap (cf. Fig. 21). An appropriate, observable OP for the HO that follows from our model could be derived from the macroscopic average of an even function of $M_z(t)$. As mentioned above, the FS gap is such an even function, $\Delta(t) \propto |M_z(t)|$. Assuming for the temperature dependence of the mode $M_z(t) = M_0(T) \cdot \cos(\omega t)$, this gives for the temperature dependence of the averaged, macroscopic gap $\bar{\Delta}_{\text{HO}}(T) \propto M_0(T)$. Consequently, if the amplitude of the mode $M_0(T)$ behaves as an OP, the macroscopic, time-averaged gap $\bar{\Delta}_{\text{HO}}$ should be expected to behave as an observable OP. Two experimental techniques, point contact and far-infrared optical spectroscopy revealed that the HO gap does indeed approximately behave as a typical BCS-type order parameter with temperature.^{110,131,132} Very recent STS measurements have unambiguously demonstrated this feature.^{56,91} We remark that in contrast to standard BCS theory the here-obtained FS gap is not symmetric around E_F , see Fig. 5.

A second possibility for an even function of $M_z(t)$ would be the dynamical susceptibility, expressed by the (longitudinal) dynamical spin-spin correlation function,

$$S(\mathbf{q}, \omega') \propto \sum_{i,j} e^{i\mathbf{q} \cdot (\mathbf{R}_i - \mathbf{R}_j)} \int e^{-i\omega' t} \langle S_{z,i}(t) S_{z,j}(0) \rangle dt, \quad (2)$$

where $S_{z,i}$ is the z component of the spin operator at the U position \mathbf{R}_i . For relativistic materials such as actinides, it is more appropriate to use the total angular momentum, i.e., $\langle J_{z,i}(t) J_{z,j}(0) \rangle$. Approximating $\langle J_{z,i}(t) J_{z,j}(0) \rangle \approx \langle J_{z,i}(t) \rangle \langle J_{z,j}(0) \rangle$, i.e., as $M_{z,i}(t) M_{z,j}(0)$, and using for \mathbf{q} the AF wave vector \mathbf{Q}_{AF} , the dynamical spin-spin correlation function $S(\mathbf{q}, \omega')$ would show a resonance peak at $\omega' = \omega$ that would be detectable in inelastic neutron experiments. Computing the frequency-integrated area of the peak, $A = \int S(\mathbf{Q}_{\text{AF}}, \omega') d\omega'$, it follows that $A(T) \propto M_0^2(T) \propto \bar{\Delta}^2(T)$. Hence, the area of the inelastic neutron peak at the AF wave vector was predicted²⁴ to behave as a secondary OP; on account of its form with a temperature-behavior different from $\bar{\Delta}_{\text{HO}}$. A very recent study of the inelastic AF resonance confirms that the area of the inelastic peak indeed displays OP behavior.³⁵ Further investigations of its temperature behavior are warranted to determine its precise contour. In the LMAF phase the AF mode ceases to exist and hence the inelastic peak area vanishes. Adopting the spin-spin correlation function expressed through the inelastic peak area A as a derived OP for the HO phase, one obtains the situation where the staggered AF moment $M_z \neq 0$ and $A = 0$ in the LMAF phase while conversely $M_z = 0$ and $A \neq 0$ in the HO phase, i.e., the phases have distinct OP's (cf. the discussion regarding this in Refs. 1, 33, 86, and 133–135).

Interestingly, so far only the gap Δ_{HO} and the inelastic neutron peak intensity A were proven to display typical OP behavior.^{35,56} Both quantities are evidently related to the intense AF mode in the HO phase, emphasizing that the AF mode is essential for the HO. Earlier ²⁹Si NMR experiments¹³⁶ on an oriented powder sample indicated that the NMR line width displayed $S = 1/2$ mean-field OP behavior in the HO phase. Later ⁹⁹Ru NMR measurements¹³⁷ also

suggested an increase in the linewidth below T_0 . Another NMR experiment, however, observed an inhomogeneous development of AF order below T_0 ,¹³⁸ and a further NMR experiment did indeed detect an increase in the linewidth below T_0 but this effect disappeared at lower temperatures and more strain-free crystals.⁴⁴ Hence, it cannot be excluded that in the early NMR measurements some inhomogeneity causing small AF patches could have influenced the result.

Second order phase transitions are characterized by a divergence of a (generalized) susceptibility at the critical temperature. We note that the critical behavior of the dynamical susceptibility $\chi(\mathbf{q}, \omega)$ at the HO transition is consistent with the proposed importance of spin fluctuations. Its imaginary part χ'' is proportional to the spin-spin correlation function, $S(\mathbf{q}, \omega)$. Its real part $\chi'(\mathbf{q}, \omega)$, however, was found—from inelastic neutron experiments—to exhibit a sharp cusp at $\mathbf{q} = \mathbf{Q}_{\text{AF}}$ and $\omega \approx 0$ when entering the HO.¹³⁹ This signals a divergence of $\chi'(\mathbf{Q}_{\text{AF}}, \omega \approx 0)$ at T_0 , which has been broadened only by experimental resolution.

The magnetic fluctuations could also bear relevance²⁴ to the occurrence of unconventional^{45–47} SC out of the HO at temperatures below 1.2 K.^{7–9} The persistence of spin fluctuations at the incommensurate wave vector down into the SC phase was observed by Broholm *et al.*^{39,42} A very recent inelastic neutron study¹⁴⁰ reveals a small energy shift in the AF mode upon entering the SC phase, suggesting an involvement of the AF spin excitations in mediating the SC.

2. Symmetry breaking

Static AF ordering obviously corresponds to breaking of time-reversal symmetry and of the body-centered translation vector in the LMAF phase; the latter causes mainly a doubling of the unit cell along the c axis. What would be the symmetry breaking induced by the longitudinal AF mode? The unconventional answer is that it in fact depends on the time scale being considered. On a very short time scale, typically much less than that of one oscillation, the body centering as well as time invariance will “instantaneously” be broken. On a sufficiently long time scale however the moments on both uranium atoms have reverted their orientation many times, and thus the two atoms are no longer distinguishable. As the two U atoms are undistinguishable on long time scales there will, consequently, be no breaking of time-reversal symmetry nor of the body-centered translation vector. Alternatively, this can be assessed, for example, from the moment-moment correlation function [Eq. (2)], which is time even. Most experimental techniques probe quantities on relatively long time scales, much longer than picoseconds (e.g., μSR or elastic neutrons). These will not be able to detect a symmetry breaking in the HO phase.

The question whether time-reversal or possibly translational symmetry is broken in the HO is an issue of on-going debate. Earlier neutron experiments provided evidence for the breaking of time-reversal symmetry,⁴³ however these measurements might have been influenced by the presence of parasitic small moments. Also later, more precise neutron experiments deduced evidence for time-invariance breaking,^{133,134} yet the issue is not unambiguously settled. Newer ²⁹Si NMR on single crystals detected a small line

shift as well as a linewidth enhancement below T_0 which corresponds to the presence of a small internal magnetic field.¹⁴¹ This finding might indicate the presence of time-invariance breaking in the HO phase. Also, the temperature-dependent static magnetic susceptibility of URu_2Si_2 displays a clear kink at T_0 .^{11,142,143} Such feature is not uncommon at an AF ordering transition in actinide compounds, and it indicates the influence of a magnetic field on the HO. This in turn could suggest that a purely electric OP such as an electric quadrupole or hexadecapole is unlikely. Electric hexadecapolar order has been proposed for $\text{PrRu}_4\text{P}_{12}$ precisely because of the observed insensitivity of an ordering transition to a magnetic field.¹⁴⁴

Altogether, clear experimental evidence for either breaking of the time-reversal or the translational symmetry in the HO phase is so far lacking. A possible verification of the symmetry breaking due to the AF mode would require a sufficiently fast experimental technique, such as x-ray scattering or photoemission. The here-proposed breaking of the body centering could be probed in ARPES experiments, where the corresponding doubling of the unit cell would appear as a sudden folding of bands at T_0 , together with a change in the c^* axis periodicity. A further argument in favor of time-reversal and translational symmetry breaking in the HO might come from dHvA and SdH experiments. The theoretical FS (Fig. 17) computed for the symmetry-broken phase agrees well with the inferred experimental FS. This correspondence suggests that the body-centered translation vector is broken in the HO phase and most likely the time-reversal symmetry as well. Conversely, using the FS computed for the bct phase, it is not possible to explain the observed dHvA and SdH quantum oscillations.^{36,92,105} Although this is consistent with the dynamical symmetry-breaking model, it cannot be excluded that other mechanisms for the HO lead to the same symmetry reduction.

V. DISCUSSION

It is elucidative to consider if hidden order phases have been discovered in other $5f$ materials. Apart from URu_2Si_2 , the actinide dioxide NpO_2 has drawn considerable attention^{6,145–147} because a sharp phase transition to an unusual phase occurs below 30 K as is witnessed by specific-heat measurements.¹⁴⁸ Intensive research during the last two decades revealed that, in the absence of any magnetic dipole moment, long-range multipolar ordering of a higher order magnetic multipole (octupole or higher) on the Np ions is likely to occur in the unusual phase below 30 K.^{6,145} These higher multipoles cannot be observed experimentally but electric quadrupolar order appearing as a *secondary* OP has been observed through resonant x-ray scattering (RXS) (Ref. 145) and ¹⁷O NMR.¹⁴⁹ Theories based on $5f^3$ localized states on the Np^{4+} ion have further provided insight in the multipolar order.^{6,150}

Also for URu_2Si_2 a number of theories for the low-temperature order have been developed on the basis of localized or nearly localized $5f^2$ configurations. Specifically, for URu_2Si_2 the following multipolar OPs have been proposed: electric quadrupole,^{14,28,50} magnetic octupole,^{19,21,23,51} elec-

tric hexadecapole,^{14,26} and magnetic triakontadipole.²⁷ Other theories on the basis of CEF considerations for a $U^{4+} 5f^2$ ionic state have also been developed.^{16,49} Electric quadrupolar ordering should be detectable with RXS,¹⁴⁵ yet experimental studies gave a null result.^{151,152} Quadrupolar order requires an E_1 - E_1 scattering channel to be detected, whereas higher order multipoles require at least an E_2 optical transition. Since the scattering cross section for E_2 transitions is extremely small, a detection of higher order multipoles is currently unlikely. Furthermore, most of these theories are based on a localized $U 5f^2$ configuration, but in spite of a similarity in the thermodynamic properties of URu_2Si_2 and NpO_2 , treating the $5f$'s as localized in NpO_2 is a good approximation,¹⁵³ but it is questionable if this approximation is valid for URu_2Si_2 , too.

Triakontadipolar order in the HO phase of URu_2Si_2 was recently proposed²⁷ on the basis of LSDA+ U calculations with a Coulomb U of about 1 eV. In contrast to localized $5f^2$ theories, the f electrons are relatively delocalized in this description. These LSDA+ U calculations predict an unusual long-range ordered AF state for URu_2Si_2 with *parallel* spin and orbital magnetic moments.¹⁵⁴ URu_2Si_2 is an unconventional material and it might indeed be that such an unusual magnetic state is realized. It should be noted however that thus far not a single magnetically ordered U compound has been discovered having this property. This can be understood from the strong spin-orbit interaction in actinides, which enforces always antiparallel spin and orbital moments in the early actinides. Also, conventional LSDA calculations predict antiparallel spin and orbital moments,²⁴ and, as mentioned above, antiparallel spin and orbital moments are in fact consistent with neutron form factor measurements.⁹⁸ Moreover, the experimental values deduced for the separate spin and orbital moments are in close agreement with values predicted by LSDA calculations. The Fermi surface predicted by LSDA+ U calculations deviates already substantial from the LSDA FS. In particular, new band crossings appear and the FS gapping feature is lost (cf. Fig. 10); thus, the LSDA+ U approach with a U of more than 1 eV cannot explain the FS gapping appearing in the LMAF phase. The recent LSDA+ U calculations²⁷ predict that, with expansion of the lattice parameter a , a phase transition would occur in URu_2Si_2 from the AF ordered phase to the same AF ordered phase but with both spin and orbital moments being opposite to the original ones. The triakontadipolar moment is predicted²⁷ to be present in both AF phases, but it could become the main OP precisely at the transition point between these two AF phases, where the dipolar moment would vanish. It should be noted, however, that such a phase transition from one AF to another AF phase, being identical by symmetry has not been observed in URu_2Si_2 . Also the predicted^{27,154} parallel spin and orbital moments are not supported by experimental observations.

Electric hexadecapolar order in URu_2Si_2 has been considered on the basis of a CEF Hamiltonian¹⁴ and more recently on the basis of DMFT calculations.²⁶ Santini and Amoretti¹⁴ showed that for a $5f^2$ level scheme consisting of three singlets magnetic dipolar and electric hexadecapolar order parameters would be possible but could not reproduce the experimental features for the chosen parameter values. The

recent DMFT calculations²⁶ suggest a nearly localized $5f^2$ configuration on the uranium ion, consisting of two singlet CEF levels, separated by 35 K. The HO phase with hexadecapolar OP emerges from an excitonic mixing of the CEF ground and the first excited state singlet. The two singlet levels are the same as those considered by Santini and Amoretti¹⁴ but notably with the order of ground state and first excited state reversed. The same CEF level scheme as that used in Ref. 14 had been proposed earlier¹⁵⁵ to explain the Ising-type anisotropy and maximum of the magnetic susceptibility. Although such CEF model can indeed explain certain properties of URu_2Si_2 , it is one of the observations of the present study that on the whole the CEF model does not corroborate with many other experimental data.

The here-reported computed results suggest altogether that an applicable explanation of the properties of URu_2Si_2 ought to arise from an itinerant $5f$ electronic structure. A number of earlier HO theories^{13,17,18,20,22,156} have been based on the itinerant $5f$ picture, and more recently, two theories have emphasized the importance of dynamic spin fluctuations for the HO.^{24,25} The earlier theories^{13,17,18,20,22} could offer an explanation for some aspects of the HO but none of the models could be unambiguously confirmed experimentally (see, e.g., Refs. 38, 72, and 157 for a discussion). The two HO theories that highlight the role of dynamical spin excitations have either focused on spin fluctuations at the AF wave vector²⁴ or at the incommensurate wave vector.²⁵ Obviously, spin fluctuations at the incommensurate wave vector as proposed in the recent theory by Balatsky *et al.*²⁵ are expected to have an influence, therefore further investigations of the incommensurate mode are needed to establish the relative importance of the two modes.

In the present work we have studied particularly the effect of the AF mode and find that its presence in the HO phase can explain the FS gapping, the broken-symmetry FS, the relation $\Delta_{HO} \approx (0.7-0.8)\Delta_{LMAF}$, as well as the mean-field OP behavior of Δ_{HO} and the secondary OP behavior of the inelastic neutron peak. The dynamical symmetry-breaking model nonetheless builds on the surprising and exceptional explanation of the HO phase being driven by the dynamic AF mode. Spin excitations are usually only weak perturbations of the ground state, that in conventional materials, cannot modify the ground state nor its properties. In URu_2Si_2 , however, the exceptional situation appears to be realized that the low-lying spin excitations actually dictate the thermodynamic properties of the HO phase. Thus far a similar situation was apparently realized only in one other material, $PrAu_2Si_2$,¹⁵⁸ which has the same crystal structure as URu_2Si_2 . Why the low-lying AF spin excitations are so effective in URu_2Si_2 is related to materials' specific aspects. The calculated energy scale of AF excitations is only on the order of 7 K, but they couple to an unexpectedly large FS reconstruction, with gaps of about 700 K. Thereby these low-lying modes can essentially modify the thermodynamic and transport properties and are indeed inherent to the HO phase.

Our calculations lastly emphasize that in URu_2Si_2 several remarkable, *materials' specific* features are combined. First, the LMAF phase with its relatively modest total moment has a total energy that is very close to that of the PM phase. Second, the low-temperature FS of URu_2Si_2 supports a nest-

ing vector \mathbf{Q}_{AF} that promotes long-range AF ordering or longitudinal AF spin fluctuations. Third, the energy bands in the ST BZ exhibit accidental degenerate crossing points at E_F as well as close to E_F . Fourth, a breaking of the body-centered translational symmetry together with time-reversal symmetry breaking in the LMAF phase or through longitudinal spin fluctuations causes a lifting of the degeneracy at the Dirac points and thus to the opening of a partial gap. These observations underline that to a large extent the HO is not a generic property but rather, it is borne out of the materials' specific electronic structure.

VI. CONCLUSIONS

For a quarter century the mysterious hidden order phase in URu_2Si_2 has been in the focus of many investigations. A detailed understanding of the underlying electronic structure of URu_2Si_2 in both the PM and LMAF phases is required before a full explanation of the HO can be formulated. Neither the PM nor the LMAF phase appear to be exceptional, therefore first-principles electronic structure calculations should be capable of explaining the known solid-state properties of these two phases. Using *ab initio* electronic structure calculations on the basis of the DFT-LSDA/GGA, the GGA+ U , and LDA+DMFT methodologies, we have performed an extensive study of the electronic structure of URu_2Si_2 . A major question has for a long time been what the applicable electronic structure of the PM and LMAF phases is, whether it has itinerant or localized uranium $5f$ electrons or perhaps $5f$ electrons with dual, i.e., both itinerant and localized characteristics (cf. Ref. 69). Our conclusion regarding this issue is that we obtain an electronic structure picture consistent with available experimental data only when we adopt delocalized $5f$ states.

Specifically, we find that materials' specific DFT-LSDA/GGA electronic structure calculations on the basis of delocalized $5f$'s explains the following low-temperature properties of URu_2Si_2 : (1) the equilibrium volume, (2) the internal z_{Si} coordinate and c/a ratio, (3) the bulk modulus and equation of state, (4) the spin and orbital magnetic moment of the LMAF phase, (5) the closeness in total energy of the PM and LMAF phases, with the LMAF phase becoming more stable under pressure, (6) the Fermi-surface gapping and instability, (7) the compensated metal character, (8) the number of holes, (9) the $5f$ occupation number, (10) the resistivity jump at the PM to LMAF transition, (11) crystallographic anisotropy of the resistivity, (12) the gapping in the infrared optical spectra, (13) the antiferromagnetic and incommensurate FS nesting vectors, and (14) the dHvA and SdH frequencies, as well as their angular dependence. In contrast, assuming a localized uranium $5f^2$ configuration we cannot obtain a satisfactory explanation of the experimental low-temperature data.

The recent ARPES data⁶⁷ form a notable exception to the set of low-temperature properties that are explained by $5f$ itinerant electronic structure calculations. A (nearly) localized $5f^2$ uranium configuration appears to tally better with the observed spectral features.²⁶ As the Fermi surface detected through ARPES evidently has to match that obtained with quantum oscillation techniques, more experimental investigations appear to be needed to resolve this issue.

We have additionally studied URu_2Si_2 in the high-temperature PM phase, using LDA+DMFT calculations. Our DMFT calculations predict the progressive opening of a quasiparticle coherence gap at the chemical potential when temperature is reduced toward the coherence temperature.

An explanation of the hidden order requires still taking a step beyond conventional electronic structure calculations, however, the electronic structure picture underlying any explanation of the HO phase must be consistent with those underlying the PM and LMAF phases. The current investigations strongly emphasize that a well-grounded explanation of the HO has to emerge from an itinerant f -electron picture. From the presented calculations we conclude that the presence of the intense AF mode in the HO phase could explain (i) the FS gapping occurring in the HO phase, (ii) its broken-symmetry FS extremal orbits and incommensurate nesting vector, (iii) the experimentally found relation between the gaps in the HO and LMAF phases, $\Delta_{\text{HO}} \approx (0.7-0.8)\Delta_{\text{LMAF}}$, and (iv) the OP behavior of the gap Δ_{HO} and the secondary OP behavior of the inelastic dynamical susceptibility. The dynamical symmetry-breaking model appears so far to be the only theory that explains and even predicted²⁴ these four properties. The importance of this mode for bringing about the HO transition is further exemplified by its occurrence and gapping in its magnon dispersion, its assistance in the entropy removal, as well as the divergent behavior of the staggered susceptibility χ' at T_0 . The presence of the inelastic AF mode at low temperatures, down into the SC phase,¹⁴⁰ could provide a clue as to why an unconventional form of superconductivity develops.

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